## Functions

This problem gives you the chance to:

- work with graphs and equations of linear and non-linear functions

On the grid are eight points from two different functions.

- four points fit a linear function
- the other four points fit a non-linear function.

For the linear function:
1.Write the coordinate pairs of its four points.
$\qquad$
$\qquad$
$\qquad$
$\qquad$

Draw the line on the grid.

2.Write an equation for the function.

Show your work.
$\qquad$

For the non-linear function:
3. Write the coordinate pairs of its four points.
$\qquad$
$\qquad$
$\qquad$

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Draw the graph of the function on the grid.
4.


Chris

Who is correct?
Explain your reasons.

$\qquad$
$\qquad$
$\qquad$
$\qquad$
$\qquad$
5. Write an equation that fits the non-linear function.

Show your work.

| Functions | Rubric |  |
| :---: | :---: | :---: |
| The core elements of performance required by this task are: <br> - work with graphs and equations of linear and non-linear functions <br> Based on these, credit for specific aspects of performance should be assigned as follows | points | section points |
| 1. Gives correct answers: $(2,9),(3,7),(4,5),(5,3)$ and <br> Draws a correct line on the grid. | 1 | 1 |
| 2. Gives correct answer: $\mathbf{y}=\mathbf{1 3 - 2 x}$ | 2 | 2 |
| 3. Gives correct answers: $(\mathbf{1}, \mathbf{5}),(\mathbf{2}, \mathbf{8}),(\mathbf{3}, 9),(4,8)$ Draws a correct curved graph or equivalent | $\begin{aligned} & 1 \\ & 1 \end{aligned}$ | 2 |
| 4. Gives correct answer: Chris <br> and <br> Gives a correct explanation such as: The graph has a turning point. or It is part of a parabola. | 1 | 1 |
| 5. Gives correct answer: $y=6 x-x^{2}$ or equivalent such as $-(x-3)^{2}+9$ <br> Shows some correct work such as: <br> Substitutes coordinates in $y=a x^{2}+b x+c$ | $1$ <br> 1 | 2 |
| Total Points |  | 8 |

Functions
Work the task and look at the rubric. What strategies or big mathematical ideas might students use to help them f nd the formulas for part 2 ar5d

Look at student work for part one. How many of them were able to pick the correct points?
How many put $(2,8)$ instead of $(2,9)$ ? $\qquad$ What other misconceptions or errors did you notice for this part?

Now look at student work for part 2How many of your students:

| $y=13-$ <br> $2 x$ | $y=$ <br> $m x+b$ | An expression with <br> $-2 x$, incorrect <br> constant | Numerical <br> expression, no <br> variable | Table or <br> list of <br> points | Other |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |

What does each answer show about that students understand about equations? Variables? Checking more than one set of points? Connecting algebraic and graphic representations? How many of your students were unwilling to attempt an equation? $\qquad$ Make a list of the types of strategies students used to solve this part of the task.

Were there strategies that you might have expected them to use that you didn't see? Which strategies most consistently gave the correct answers?

Now look at the graphs for part 3 . How many of your students selected the correct 4 points?
How many could visualize the points as a parabola? $\qquad$ How many connected the points in a pointy shape? $\qquad$ How many tried to make a quadrilateral? $\qquad$ How many made a square shape? $\qquad$ What experiences have your students had with graplgiparabolas? Do students get an opportunity to explore how dif er parts of the equation ef ect the shape of the graph?

Now look at the explanations for quadratic and exponential equations. How many of your students could give:

- a reasonable explanation?
- were unwilling to answer? $\qquad$
- thought exponential meant exponents in the equation? $\qquad$
- thought quadratic meant 4 points or asfided $f$ gure? $\qquad$
Algebra-2008
- the graph isn't square, so it can't have square numbers? $\qquad$
- thought boh answers were correct? $\qquad$
How do we help students develop academic language? How often do students have discussions in class where they need to use these words to help express their ideas? How do we help orchestrate or foster their experiees?
Finally look at student work for part 5. How many of your students put:
- $y=6 x-x^{2}$ ? $\qquad$
- an equation with $\bar{x}$ ? $\qquad$
- a linear equation, that would f tone of the points? $\qquad$
- attempted to use a table?
- tried $a x^{2}+b x+c$, but couldn't get to a f nal answer? $\qquad$
- a numerical expression? $\qquad$
- no attempt? $\qquad$
- other? $\qquad$

What thinking did you see, whether successful or not, that could be built upon in future lessons?
In what way could you use some partial student work to push students to do more investigation around this idea? Were there any problem solving strategies that were worth talking about?

## Looking at Student Work on Functions

Student $A$ is able to think about the equation of anne and use it to $f$ nd the equation in part 2. Notice how the student calculates the slope and then extends the graph to think about the yintercept. In part 4 the student has the language to talk about quadratic functions. Notice that the student has addean additional point on the graph to make the parabola symmetrical. In part 5 the student uses the formula for the turning point of a parabola to check that the equation is correct.
Student A
On the grid are eight points from two different functions.

- four points fit a linear function
- the other four points fit a non-linear function.

For the linear function:

1. Write the coordinate pairs of its four points.


Draw the line on the grid.

2. Write an equation for the function.

Show your work.

$$
\begin{array}{rl}
y=m \times t b & y
\end{array} \quad=-2 x
$$

For the non-linear function:
3. Write the coordinate pairs of its four points.


$$
(2,8)
$$

$\square$
$\qquad$

Student A, part 2


Alex

Explain your reasons.


$$
-9+18=9
$$

5. Write an equation that fits the non-linear function. Show your work.

$$
\frac{-b}{a(2)} \quad \frac{(3,9)}{-6}-3
$$



Student B shows an interesting thoughtrocess, starting with a table to look at dif erences to f nd the turning point. The student thinks about the direction of the parabola. So, using a variety of pieces of knowledge the student is able to put together a correct equation. Notice that the stueht checks the equation against all the given points.

Student B


Student C comes up with an alternative equation for the parabol\&Vhat clues can you f nd about the student's though process?
Student C Chris

Who is correct? $\qquad$ Chars
$\qquad$

Explain your reasons.
The graph
5. Write an equation that fits the non-linear function.
 Show your work.

$$
\begin{aligned}
& y=-x^{2} \\
& -1,1 \quad y=-(-x+3)^{2}+9 \\
& y=-x^{2}+9 \\
& y=16
\end{aligned}
$$

Student D is able to use slope to $f$ nd the formula for part 2. In part 5 the student makes an attempt to use the-xintercepts or roots to $f$ nd the equation. Due to inaccuracy in the graph the student's formula is a little of .What do you need to know to f nd the correct roots? What could help the student see that the roots are incorrect?

## Student D

On the grid are eight points from two different functions.

- four points fit a linear function
- the other four points fit a non-linear function.

For the linear function:

1. Write the coordinate pairs of its four points.


Draw the line on the grid. $\qquad$

2. Write an equation for the function.

Show your work.


For the non-linear function:
3. Write the coordinate pairs of its four points.


Draw the graph of the function on the grid. $\qquad$

Student D, continued

## Chris

Who is correct?


Explain your reasons.

$\qquad$
5. Write an equation that fits the non-linear function. Show your work.

$$
\left.\begin{array}{r}
x \text { intercepts }-(6.66,0) \\
0 \text { or } \\
\left(6 \frac{2}{3}, 0\right) \\
\left(2 x-6 \frac{2}{3}\right)\left(-2 x+\frac{2}{3}\right) \\
\left(-\frac{2}{3}, 0\right)
\end{array}\right)
$$



C

Student E has an interesting strategy for f ding the equation in part Row would you explain the strategy and why it works?n part 5 the strategy is not so successful.Why doesn't the strategy work this time? Could it be adjusted to ft this new situation? Student E makes the common error of connecting exponents with exponential function. Student E
2. Write an equation for the function. Show your work.
$3=-2(5)+b$


## Student E, part 2

## Chris

Who is correct? $\qquad$ t
xplain your reasons.
The non-linear function is exponential because if

zarapola.
rite an equation that fits the non-linear function. now your work.


$$
\begin{array}{rrr}
5=1^{2}+b & 8=2^{2}+b \\
5=1+b & 8 & -4+b \\
b=4 & b=4 & 2 x^{2}+3 \\
& 9=3^{2}+b \\
& b=0
\end{array}
$$

Student $F$ tries to use the slope to f nd the equation impart 5. How would you describe the misconception of the student? Why is this equation incorrect? What question could you pose to help the student see his misconception?

## Student F

5. Write an equation that fits the non-linear function. $-x+12=y \times x$ Show your work.

$$
\begin{aligned}
& \frac{8.9}{4-3}=-1 / 1 \quad m=-1 \\
& -1=\frac{y-8}{x-4} \quad+\frac{-x+4}{+8}=y-8 \\
& y=-x+12
\end{aligned}
$$

## Student G is able to complete correctly parts 1,2, and 3 of the task. Ipart four the student seems to see quadratic and exponential as describing the same function. In part 4 the student doesn't think about the writing an equation for the parabola in the f rst graph, but gives a general example complete with graph. <br> Student G



Alex

Explain your reasons.

parabola.
5. Write an equation that fits the non-linear function.

Show your work.


Many students tried to use something about slope or substitution to f nd the formula for the quadratic. Student $H$ uses the $y=m x+b$ for all the points to $f$ nd the constant in part 2. In part 4 the student states that quadratic equations can be factor®d. the student tries the same strategy for the linear equation to $f$ nd the constant in the quadratic. Notice the guess and check show factored expressions but the $f$ nal answer is a linear equation. What might be next steps for this student?

## Student H

2. Write an equation for the function.

Show your work.


For the non-linear function:

Chris
Who is correct?


Explain your reasons.
$\qquad$
is quadratic. If could te factored. A non-linear function cant be exponetial
5. Write an equation that fits the non-linear function. Show your work.

$$
\begin{array}{ll}
5=3(1)+5 & 8=3(2)+2 \\
5=3+6 & 8=6+2 \\
3-5 & 8=8 \\
2=0 & 6 \\
(3 x+2)(-2 x+13) & \frac{326}{8} \\
-6 x^{2}+391 x-4 x+26 & \frac{6}{156} \\
-6 x^{2}+35 x+26 \\
\left(-6 x^{2}+39 x+4 x+26\right) \\
-3 x(2 x-13)-22 x-13) \\
(-3 x-2)(2 x-13)
\end{array}
$$



Student I tries similar ideas, but makes an error in part 2. In part three the student just puts in all the points to try to $f$ nd the slope. Notice that the student seems to use the number line to think about combining positive and negative numbers.
Student I

5. Write an equation that fits the non-linear function. Show your work.


Student J is able to pick out the correct points in part 3 but draws the parabola at an angle. This leads to confusion on part 4. The student does have the habit of mind to test out formulas and check them. Notice all the work in part 5. How could you help the student investigate quadratics more? How could you pose a whole class investigation to explore the idea of how parts of the equation ef ect the shape of the graph?

## StudentJ

On the grid are eight points from two different functions.

- four points fit a linear function
- the other four points fit a non-linear function.

For the linear function:

1. Write the coordinate pairs of its four points.


Draw the line on the grid.
2. Write an equation for the function. Show your work.



## Chris

Alex
$\qquad$
Explain your reasons.
Alex is right because $y=x^{2}$ and $x=y^{2}$ are both parabola's 0
or non-linear. The one on the graph is non-linear but still add. These or non-linear. The one on the graph is non-linear but still add. These

angle in either of the 4 quadrants.
5. Write an equation that fits the non-linear function.

Show your work.


Student K attempts to f nd the formula in part 5 by lookig at the table of values. The student $f$ nd a dif erent formula for each set of points on the graph but doesn't know where to go from thereNhat question might you pose to push the students thinking?

## Student K

2. Write an equation for the function.

Show your work.

rite an equation that fits the non-linear function. Show your work.


$$
y=\quad y=2 x^{2}+3
$$

$$
y=\frac{2 x^{2}}{2}
$$

$$
y=\frac{2 x^{2}}{4}
$$

$$
y=\frac{2 x^{2}}{4}
$$

## Student L understands the general eqtion for a quadratic and attempts to

 substitute points into the equation. The student does not know how to solve from there. Is there a way of building on this idea to get a solution?
## Student L

On the grid are eight points from two different functions.

- four points fit a lincar function
- the other four points fit a non-linear function.

For the linear function:

1. Write the coordinate pairs of its four points.


Draw the line on the grid.

2. Write an equation for the function. Show your work.


## Student L, part 2

## Chris

Who is correct? Chris
Explain your reasons.
Chris is correct because the non-linear function graphs part of a parabola, and only quadratic equations. graph parabolas.
5. Write an equation that fits the non-linear function.

$$
\begin{aligned}
& \text { Show your work. } \\
& a x^{2}+b x+c=y \\
& a(2)^{2}+b(2)+c=8 \\
& 4 a+2 b+c=8
\end{aligned}
$$

$$
\begin{aligned}
& \text { ion. } \frac{a x^{2}+b x+c=y \times 0}{0} \\
& x=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a} \\
& 2=\frac{-b \pm \sqrt{b^{2}-4 a c}}{2 a}
\end{aligned}
$$

Algebra

## Functions

| t Task | Work with graphs and equations of linear and non-linear functions. |
| :---: | :---: |
| Coreldea 1 <br> Functions and Relations | Understand patterns, relations, and functions. <br> - Understand relations and functions and select, convert flexibly among, and use various rep resentations for them. |
| Coreldea 3 <br> Algebraic <br> Properties and <br> Representations | Represent and analyze mathematical situations and structures using algebraic symbols. <br> - Use symbolic algebra to represent and explain mathematical relationships. <br> - Judgethe meaning, utility, and reasonableness of results of symbolic manipulation. |

The mathematics of this task:

- Identify linear points on a coordinate grid and name them
- Write an equđion for a linear fundion from a graph or from coordinates
- Recognize non-linear points that form a parabola and estimate the graph of the curve
- Distinguish between features of a linear, quadratic and exponential graph and their equations
- Find the equation for a parabola given some of the coordinate points

Based on teacher observations, this is what algebra students knew and were able to do:

- Undestand that a linear graph is a straightline
- K now that a non-linear graph is a parabola
- Identifying points on a graph

Areas of difficulty for algebra students:

- Finding a linear equation from a graph
- Finding a quadratic equation
- Drawing a parabola
- Difficulty in knowing difference between quadratic and quadrilateral (fourpoint/foursides)
- Confusion aboutquadratic and exponential equations( $x^{2}$ has an exponent so it was exponential)
Strategies used by successful students:
- K nowing thegeneric formula for a line: $y=m x+b$ and using slope and substitution
- Looking for they-interceptfor the linear equation
- Finding slope
- K nowing the generic formula for a quadratic: $y=a x^{2}+b x+c$
- Knowing mathematical vocabulary: quadratic, exponential
- Extending the parabola to $f$ nd more points, particularly the roots of $x$ intercepts

Table 49: Frequency Distribution of MARS Test Task 5, Course 1

| Task 5 <br> Scores | Student <br> Count | \% at or <br> below | \% at or <br> above |
| :---: | :---: | :---: | :---: |
| 0 | 1737 | $35.6 \%$ | $100.0 \%$ |
| 1 | 381 | $43.4 \%$ | $64.4 \%$ |
| 2 | 959 | $63.0 \%$ | $56.6 \%$ |
| 3 | 528 | $73.8 \%$ | $37.0 \%$ |
| 4 | 545 | $85.0 \%$ | $26.2 \%$ |
| 5 | 399 | $93.2 \%$ | $15.0 \%$ |
| 6 | 215 | $97.6 \%$ | $6.8 \%$ |
| 7 | 79 | $99.2 \%$ | $2.4 \%$ |
| 8 | 39 | $100.0 \%$ | $0.8 \%$ |

Figure 58: Bar Graph of MARS Test Task 5 Raw Scores, Course 1


The maximum score available for this task is 8 points.
The minimum for a level 3 response, meeting standards, is 4 points.
Some students, about 64\%çuld correctly identify, name and graph the four linear points. About 56\% of the students could also name the remaining four noAlinear points. About 37\% could also graph the curve of the parabola. Only $26 \%$ could also give an equation for the linear furtion. Only 7\% could explain that the parabola was a quadratic equation. Less than one percent of the students could meet all the demands of the task including giving a equation for the parabola. Almost 36\% of the students scored no points on this task. Alout 65\% of the students with this score attempted the task.

## Functions

| Points | Understandings | Misunderstandings |
| :---: | :---: | :---: |
| 0 | $65 \%$ of the students with this score attempted the task. | Students usually knew how to order coordinate points but misread one of the points or put $(2,8)$ for $(2,9)$. Less than $3 \%$ choose all the wrong points. Less than $2 \%$ reversed the $x$ - and $y$-coordinates. |
| 1 | Students could name points on a coordinate graph, identify the ones that were linear and draw the graph. | About $6 \%$ misnamed one of the coordinate pairs for the parabola. About $9 \%$ did not attempt to name the non-linear points. |
| 3 | Students could name the linear and non-linear points and graph a straight line and a parabola. | Almost 20\% of the students made parabolas that were 4 line segments. $12 \%$ of the students did not attempt to graph these points. |
| 4 | Students could name and graph points in a linear function, give the equation of the line, and name the nonlinear points. | $17 \%$ of the students did not attempt to write an equation for the line. About $12 \%$ of the students had equations with $-2 x$ but the incorrect constant. About 5\% just wrote $\mathrm{y}=\mathrm{mx}+\mathrm{b} .5 \%$ gave numeric expressions or discrete values for x and y . |
| 5 | Students could identify and graph points for linear functions and quadratics. They could write equations for a linear function from the graph. | Students could not distinguish between quadratic and exponential equations. $25 \%$ of the students did not attempt part 4. About $12 \%$ knew that parabolas have exponents, so it should be exponential. About $5 \%$ confused quadratic with 4 sides. About $4 \%$ thought both words were the same. |
| 6 | Students could distinguish between quadratic and exponential functions. | Students struggled with the equation for the parabola. $36 \%$ of the students did not attempt this part of the task. About 5\% attempted to look at a table of values, but couldn't figure out what to do with the information. About $3 \%$ knew the general formula, $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}=\mathrm{y}$, but couldn't figure out what to do next. About $10 \%$ wrote linear equations. About $12 \%$ wrote incorrect equations with exponents. |
| 8 | Students could identify and graph linear and quadratic points and give their equations. |  |

## Implications for Instruction

Students at this grade level should be able to make connections between equations and the shape бa graph. Students should be able to recognize proportional functions $(y=m x)$ with linear equations going through the origin. Students should also be able to explain how the constant, the added portion of the equation $y=m x+b$, ef ects the graph by rasing or lowering the equation without changing the slope and also indicates the yintercept. Students should also understand that equations with exponents will not be linear. The most common form $y=m^{2} x-b x+c$ will form a parabola. Students should be ableo make predictions about the equation from looking at a graph or predictions about the graph from looking at the equation. Some students will start to move beyond this to think about quadratic equations and exponential equations or be able to write an eqtion for parabolas, but that is the ramp of this task. Students should be familiar with multiple representations and knowing how they connect to each other. Students should know how the parts of the equation relate to the shape of the graph knowing gealeform of the equations Action Research - Investigations- Linking Equations to Graphs Relationships cannot be given to students, but must be discovered through practice and exploration. In order to learn to think like a mathematician students at thisagle level need opportunities to investigate relationships. They need big rich tasks that give them opportunities to work with longer reasoning chains, learn to organize information, make systematic changes to observe the ef ects, and start to think about types of numbers and how they might ef ect outcomes. Exploring this relationship between graphs and their equations is an excellent context for investigation.

Pose a dilemma or question. For example:
I overheard two students in another class discussingraphs.
Barbara said, "All equations without exponents make straight lines." Fred added, "And they also go through zero." Don disagreed. He said that some equations without exponents don't go through zero and some are not lines." Who do you think is correct? How can you tell just by looking at an equation what a graph will look like? Can you tell how each part of the equation contributes to the shape of the graph? Organize some information that would help Barbara, Fred, and Don correct their thinking.

After students have worked with this prompt, they should make posters to share with the class or make some equations that they think might stump their classmates.

A further challenge might be to look at equations with exponents. The new prompt might be:

Find an equation that will go through $(0,0)$ and $(0,1)$.
To f nd this solution some students will be able to apply knowledge from factoring equations. Others may be led into a rich investigation in how the numbers in equations with exponents ect the shape of the graphs.

In learning a new feld of study, like algebra, students need to acquire vocabulary and procedural knowledge. But students also need the challenge and cognitive demand to work within the discipline to solve problems and makdiscoveries. They need to view the procedures and knowledge they are gaining as tools to make and test conjectures. It is the richness of exploring ideas that makes the mathematics of algebra interesting and engaging for students. It is the personal atis that make the learning satisfying and personal.

## Ref ecting on the Results for Algebra as a Whole:

Think about student work through the collection of tasks and the implications for instruction. What are some of the big misconceptions or dif culties tlt really hit home for you?
$\qquad$
$\qquad$
$\qquad$

If you were to describe one or two big ides to take away and use for planning for next year, what would they be?
$\qquad$
What are some of the qualities that you saw in good work or strategies used by good students that you wold like to help other students develop?
$\qquad$
Four areas that stand out for the Collaborative as a whole for Algebra are:

- Moving Between Multiple Representations Students had dif culty moving from graphs to equations. Students did not recognize how tsteucture of the equation would ef ect features of the graph. This was evident in both Functions and Sorting Functions.


## Performance Assessment Task Functions <br> Grade 9

The task challenges a student to demonstrate understanding of the concepts of relations and functions. A student must be able to understand functions and select, convert flexibly among, and use various representations for them. A student must be able to identify linear points on a coordinate grid and name them. A student must determine the equation for a linear function from a graph or from coordinates. A student must be able to recognize non-linear points that form a parabola and estimate the graph of the curve. A student must be able to find the equation for a parabola given some of the coordinate points. A student must be able to distinguish between the features of a linear, quadratic and exponential graph and their equations.

## Common Core State Standards Math - Content Standards

High School - Functions - Interpreting Functions
Analyze functions using different representations.
F-IF. 7 Graph functions expressed symbolically and show key features of the graph, by hand in simple cases and using technology for more complicated cases.
a. Graph linear and quadratic functions and show intercepts, maxima, and minima.

## High School - Functions - Linear, Quadratic, and Exponential Models

 Construct and compare linear, quadratic, and exponential models and solve problems.F-LE. 3 Observe using graphs and tables that a quantity inkling exponentially eventually exceeds a quantity increasing linearly, quadratically or more generally as a polynomial function..

## High School - Algebra - Creating Equations

## Create equations that describe numbers or relationships

A-CED. 2 Create equations in two or more variables to represent relationships between quantities; graph equations on coordinates axes with labels and scales.

## Common Core State Standards Math - Standards of Mathematical Practice

 MP. 3 Construct viable arguments and critique the reasoning of others.Mathematically proficient students understand and use stated assumptions, definitions, and previously established results in constructing arguments. They make conjectures and build a logical progression of statements to explore the truth of their conjectures. They are able to analyze situations by breaking them into cases, and can recognize and use counterexamples. They justify their conclusions, communicate them to others, and respond to the arguments of others. They reason inductively about data, making plausible arguments that take into account the context from which the data arose. Mathematically proficient students are also able to compare the effectiveness of two plausible arguments, distinguish correct logic or reasoning from that which is flawed, and-if there is a flaw in an argument-explain what it is. Elementary students can construct arguments using concrete referents such as objects, drawings, diagrams, and actions. Such arguments can make sense and be correct, even though they are not generalized or made formal until later grades. Later, students learn to determine domains to which an argument applies. Students at all grades can listen or read the arguments of others, decide whether they make sense, and ask useful questions to clarify or improve the arguments.

## MP. 6 Attend to precision.

Mathematically proficient students try to communicate precisely to others. They try to use clear definitions in discussion with others and in their own reasoning. They state the meaning of the symbols they choose, including using the equal sign consistently and appropriately. They are careful about specifying units of measure, and labeling axes to clarify the correspondence with quantities in a problem. They calculate accurately and efficiently, express numerical answers with a degree of precision appropriate for the problem context. In the elementary grades, students give carefully formulated explanations to each other. By the time they reach high school they have learned to examine claims and make explicit use of definitions.

## Assessment Results

This task was developed by the Mathematics Assessment Resource Service and administered as part of a national, normed math assessment. For comparison purposes, teachers may be interested in the results of the national assessment, including the total points possible for the task, the number of core points, and the percent of students that scored at standard on the task. Related materials, including the scoring rubric, student work, and discussions of student understandings and misconceptions on the task, are included in the task packet.

| Grade Level | Year | Total Points | Core Points | \% At Standard |
| :---: | :---: | :---: | :---: | :---: |
| 9 | 2008 | 8 | 4 | $26 \%$ |

