

① Kite

- Two large diagonals  
can make any parallelogram

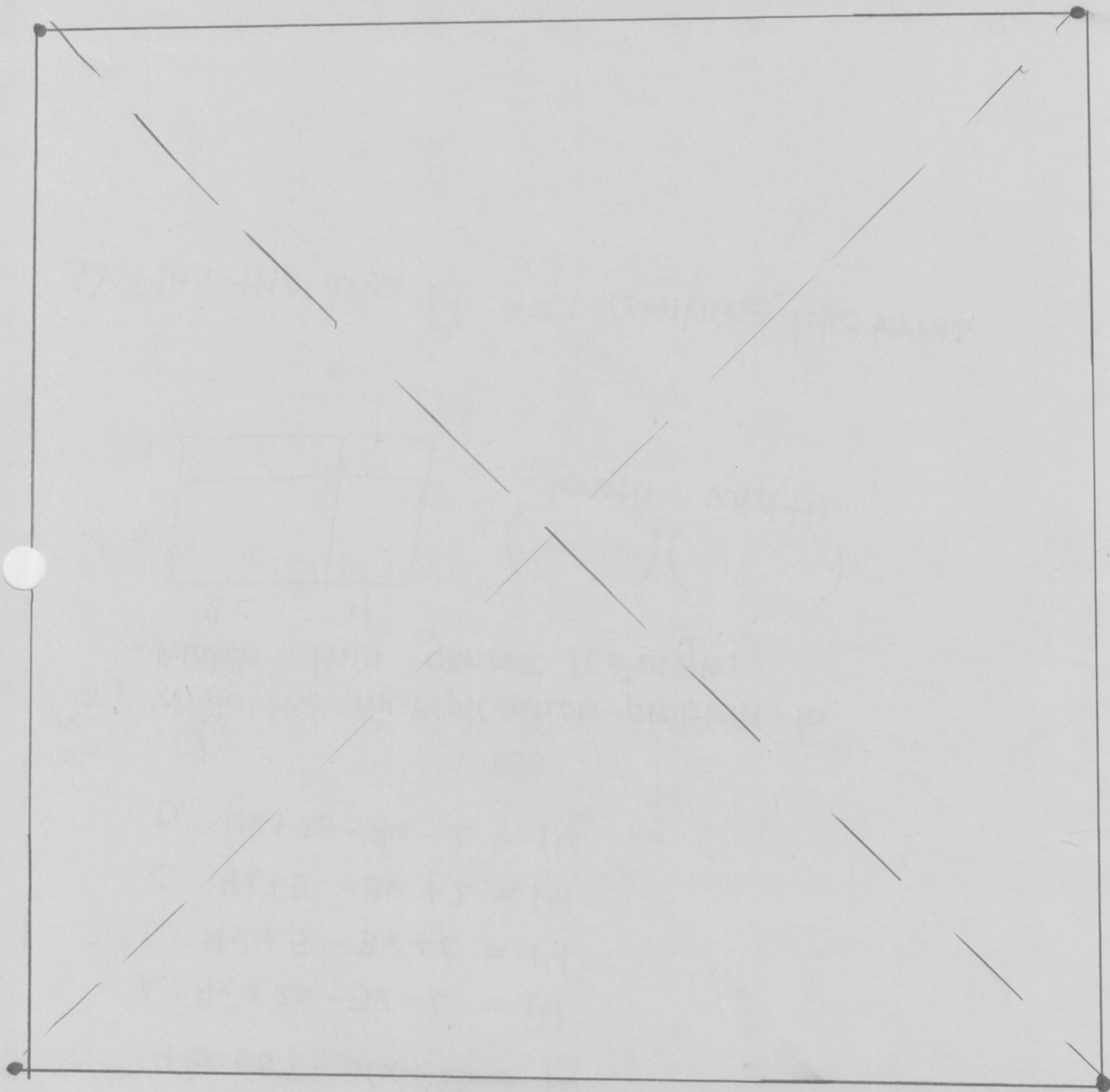
- Diagonals used in  
producing kites, rhombus,  
trapezoid or trapezium  
can not produce  
square, rectangle  
but they can  
produce a  
parallelogram

- A large diagonal &  
a short diagonal  
can make any type  
of rhombus or kite

- Any group of diagonals  
that produce a rhombus  
or kite may also be  
used to produce any  
trapezoid or trapezium.

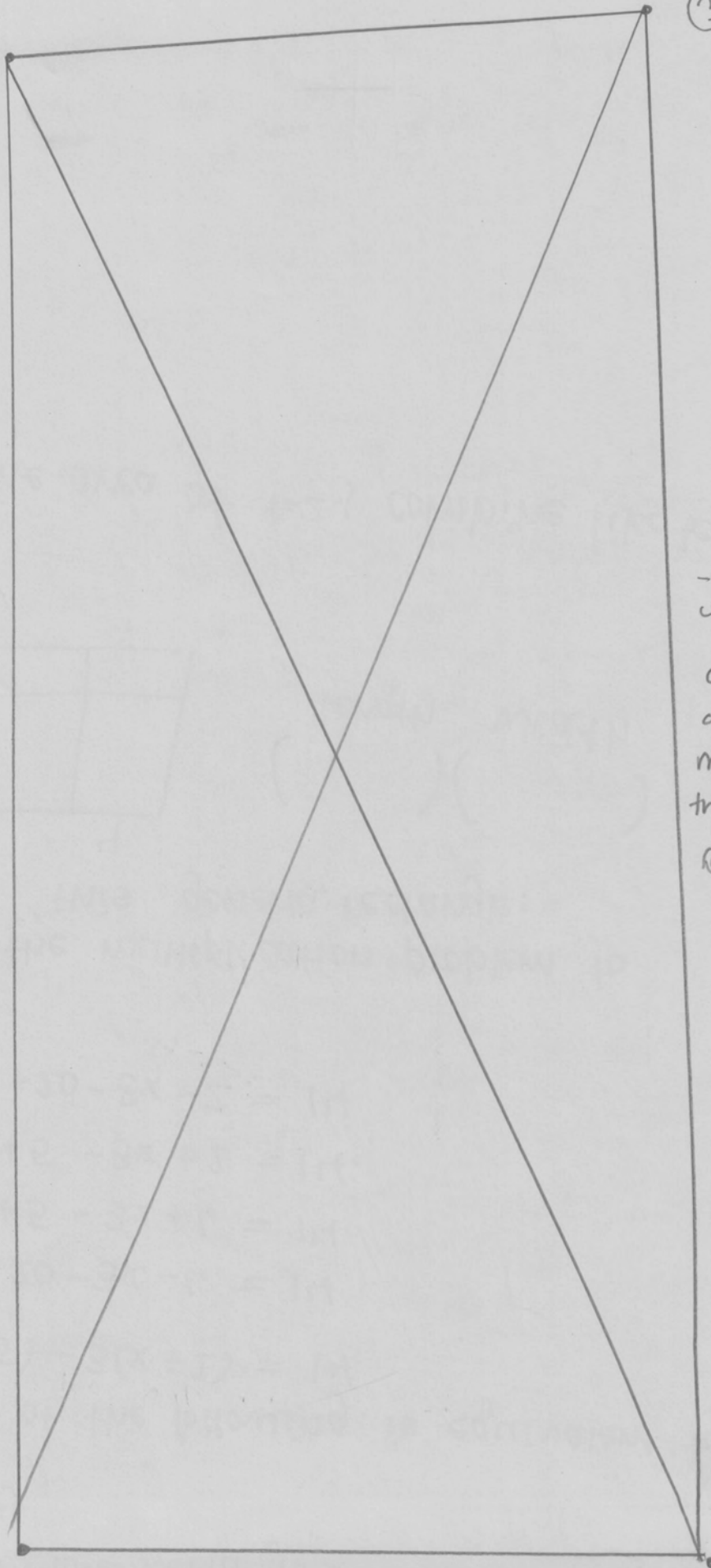
- That you CAN NOT  
stick any two diagonals  
together via there  
end points.  
(B/c it produces a  
tri.)

② square



- With 2 large diagonals you can make  
any rectangle, square or parallelogram

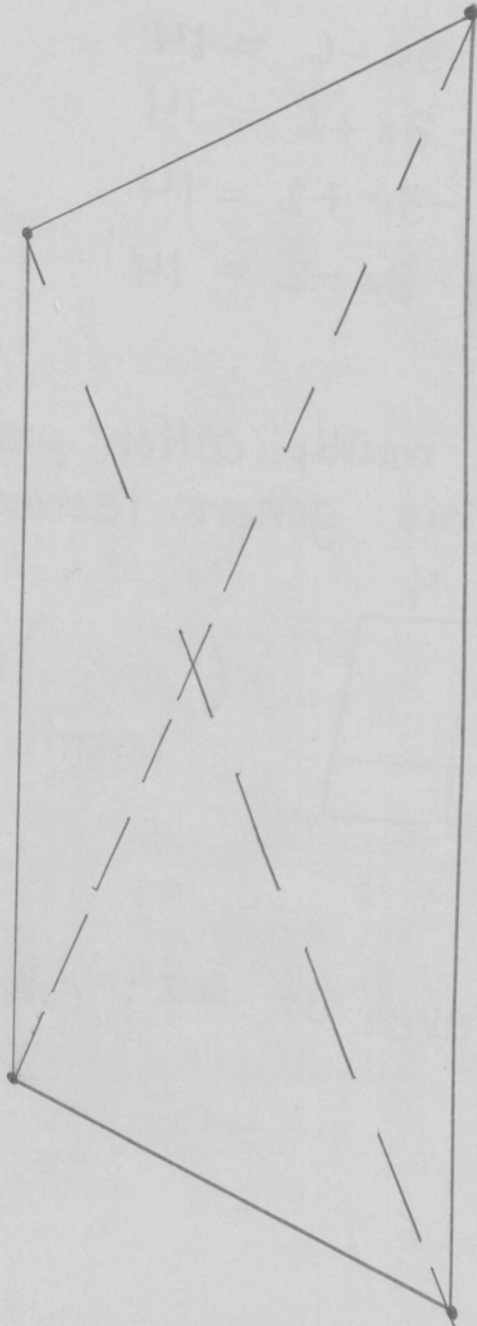
③ Rectangle



-Produced by  
using 2 large  
diagonals crossed  
at each other's  
midpoints but  
the mp do not  
form  $90^\circ$   $\angle$ .

#### 4.) Trapezoid

Everything (Every combination) of diagonals that can produce a trapezoid can also produce a trapezium.





(Supposed)

Parallelogram

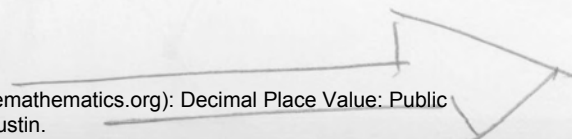
5.) Parralelogram

- A parallelogram is constructed with the use of a large diagonal connected to a short diagonal.

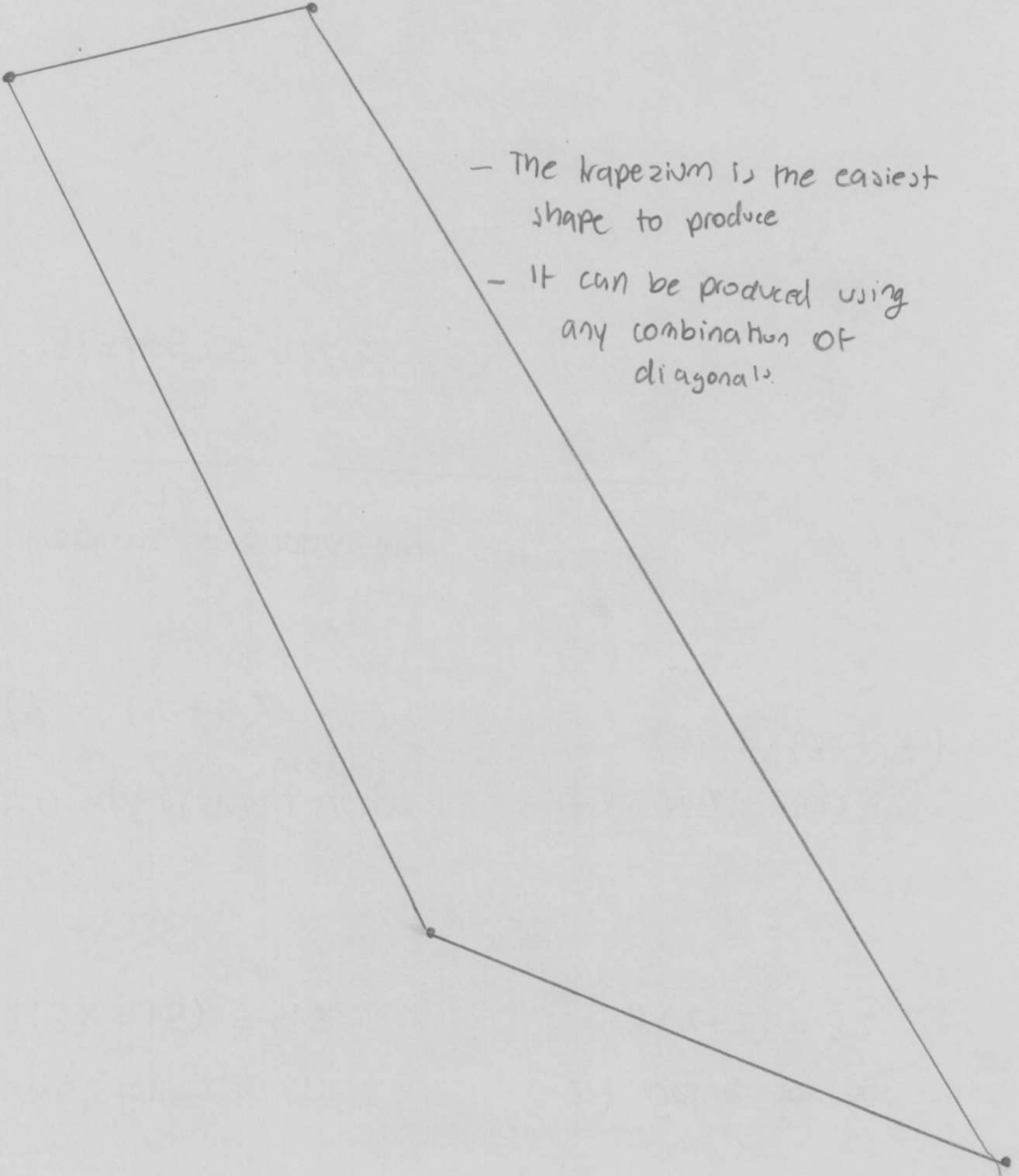


- Although most common shape is a trapezium

BACK

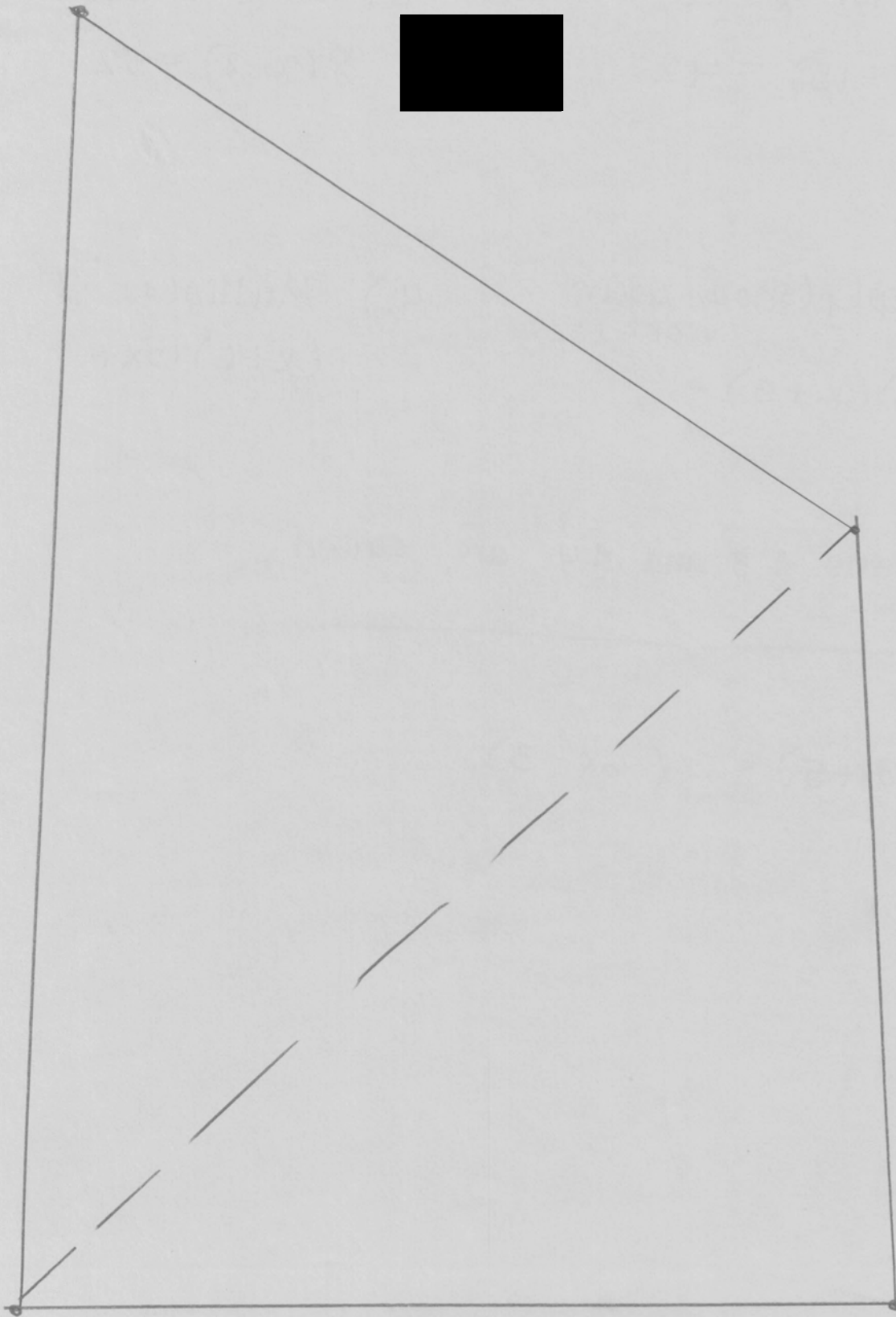


6.) Trapezium



- The trapezium is the easiest shape to produce
- It can be produced using any combination of diagonals.

7.) Different  
Trapezoid



Why is it that a rhombus can produce  
a trapezoid, trapezium, kite, & a  
parallelogram but why can't a kite?  
What other types of shapes can  
we produce that we might have  
missed?

I think that I did extremely well in documenting our process or observations.

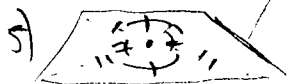
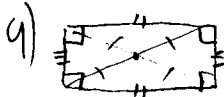
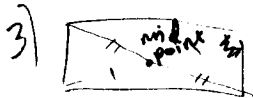
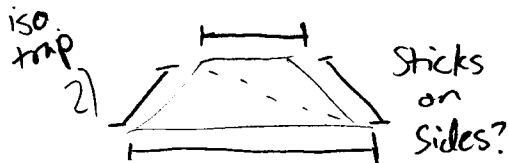
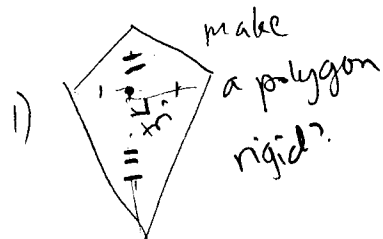
I think that I noted my observations carefully, & that my work "evolved" through my observations in a clear way.

I believe I could have improved my sketch quality a little bit b/c they seem a little sloppy.

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Mar. 3, 2009



rotated diagonals;  
one side always parallel;  
Any point will do

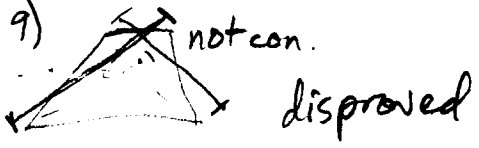
8) Sticks of diff lengths intersect; one side of the intersection must be congruent

7) Rhombus:

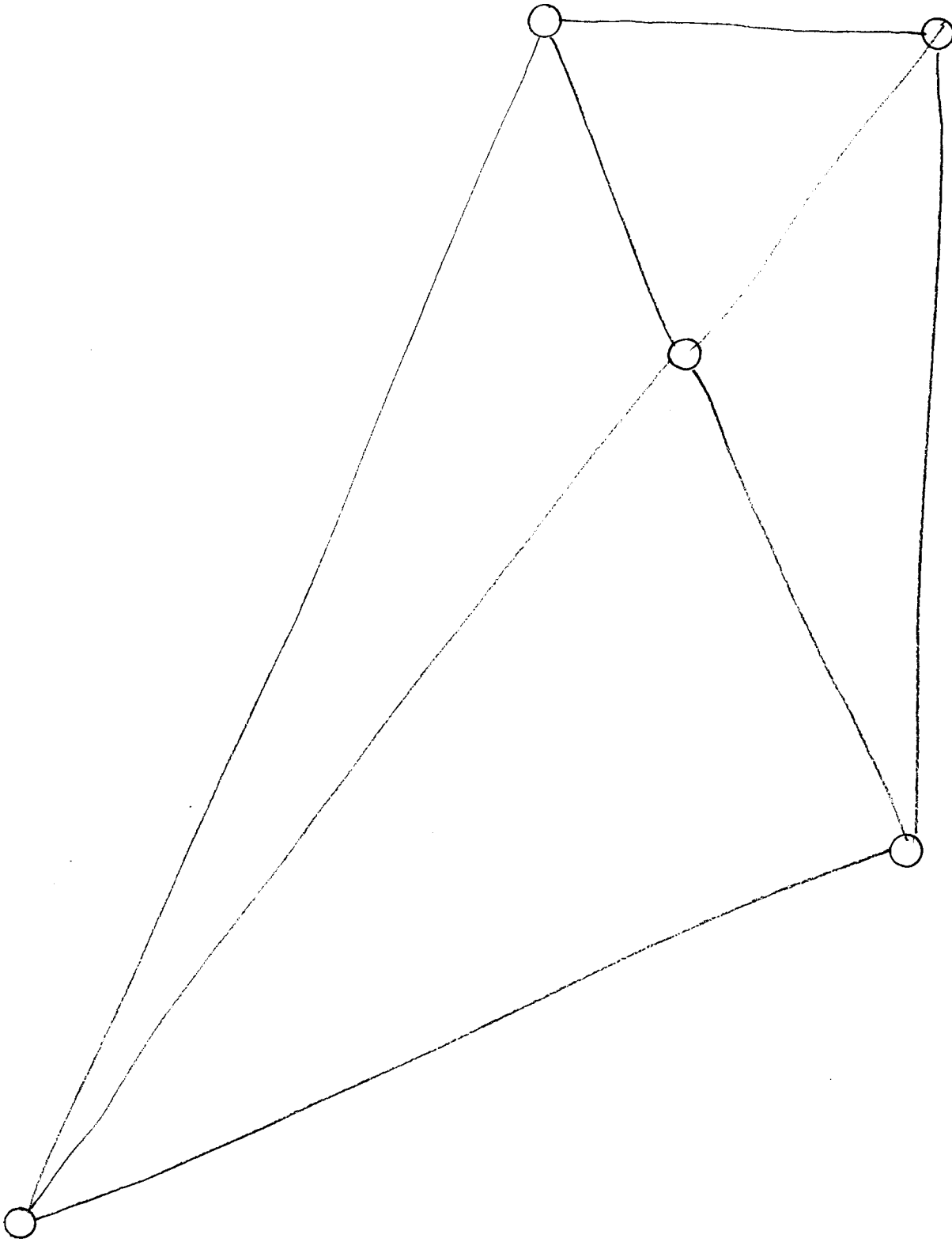
select center of one stick, place new stick on top (in center);  
despite diff in lengths of sticks the midpoint must create 2 con. segments out from intersection. sides will be parallel auto. Placed at right angles, sides  $\cong$ .

8) Parallelogram:  
One short stick, one long stick, connect both @ center.

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10)



If: the diagonals bisect each other,  
 and the <sup>diagonals</sup> are perpendicular,  
 and the diagonals are different lengths,  
 then the quadrilateral is a rhombus.

Rhombus: A parallelogram in which all sides are equal.

If: the diagonals bisect each other,  
~~and the diagonals are not perpendicular,~~  
 and the lengths are the same,  
 then the quadrilateral is a rectangle.

Rectangle: A parallelogram in which all  $\angle$ s equal  $90^\circ$ .

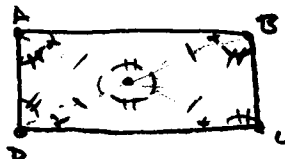
$360^\circ$  in quad

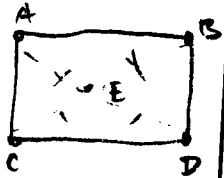
- 1) The diagonals  $\overline{DB}$  and  $\overline{AC}$  are the same length.
- 2) The diagonals' bisections are congruent ( $\overline{AE}$ ,  $\overline{DE}$ ,  $\overline{BE}$ ,  $\overline{CE}$ )
- 3)  $\triangle AEB$ ,  $\triangle AED$ ,  $\triangle BAC$ ,  $\triangle DAC$  are isosceles

- 1) Given.
- 2) Division Property of Segments
- 3) Their

Prove  $90^\circ$ : The sum of a quadrilateral's angles =  $360^\circ$   
 Addition of same angles = same angles  
 $360^\circ \div 4 = 90^\circ$

addition prop.  
of angles

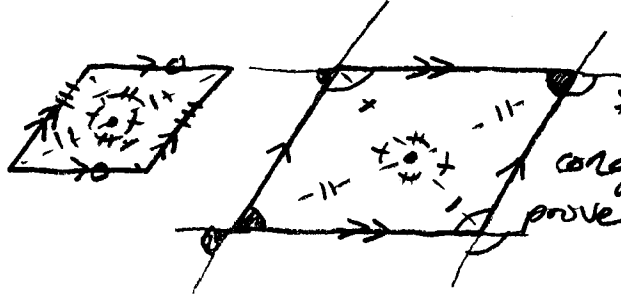
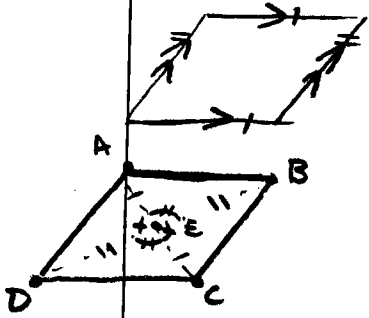




### Rectangle:

- 1)  $\overline{AD} \cong \overline{CB}$  1) Given
- 2)  $\overline{AE} \cong \overline{ED} \cong \overline{CE} \cong \overline{BE}$  2) Division Property of Segments
- 3)  $\angle AEB \cong \angle CED$  3) Vertical angles are  $\cong$ .
- 4)  $\angle AEC \cong \angle BED$  4)  $\parallel$
- 5)  $\triangle AEB \cong \triangle CED$  5)

Parallelogram:



Proving triangles congruent... won't prove the conjecture.

1)

1)



Mar. 3, 2009

How is it possible to place sticks so that they make rigid quadrilaterals and can be described as one special type or another?

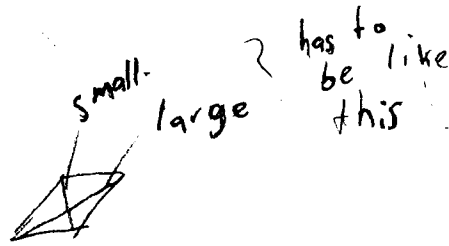
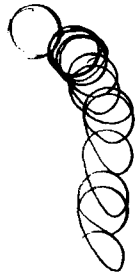
What I think I did well: state my questions, conjectures and made diagrams as I went along.

What I think I need to improve on: Recording my first observations which lead to my conjectures.

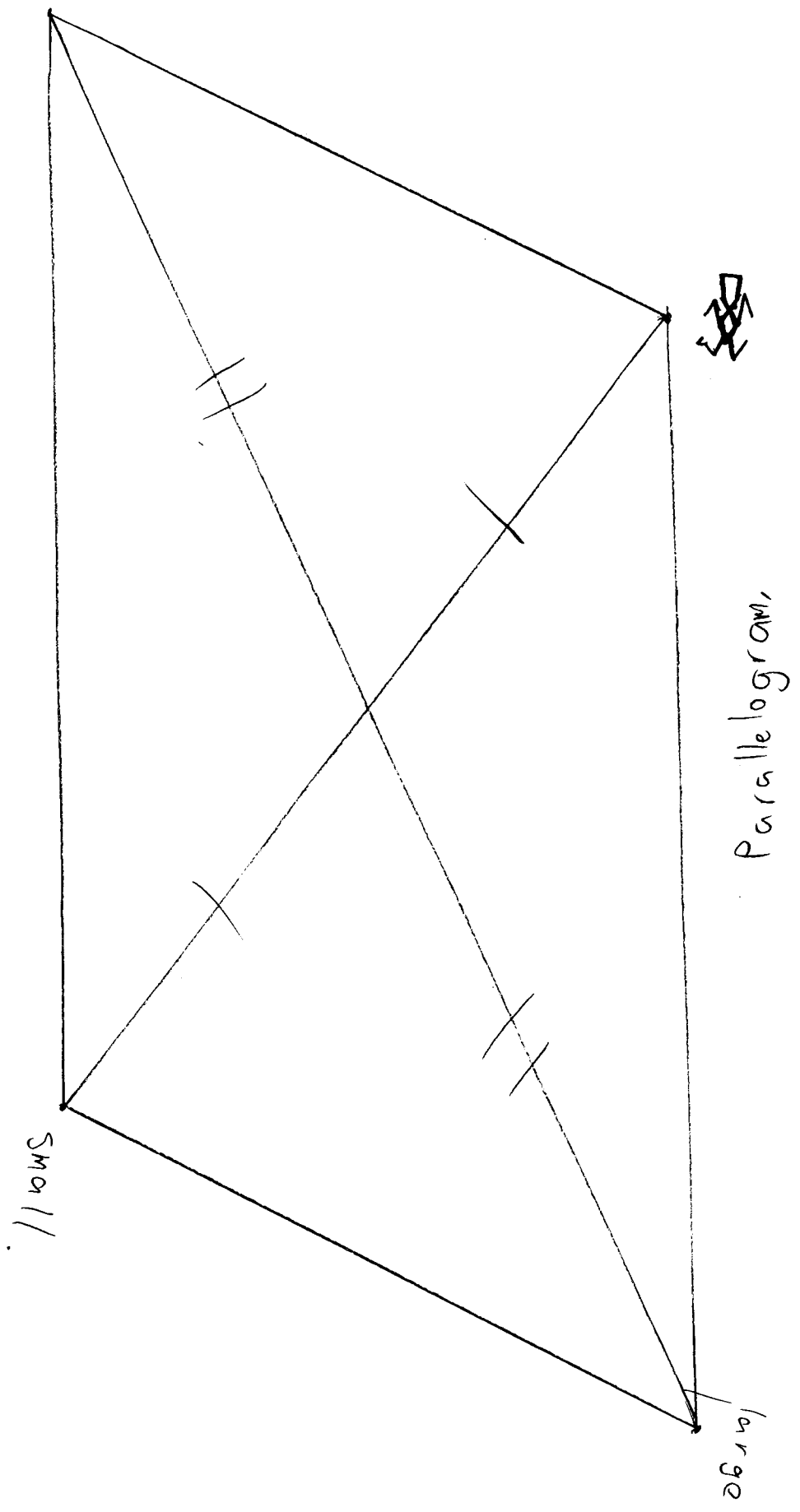
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①

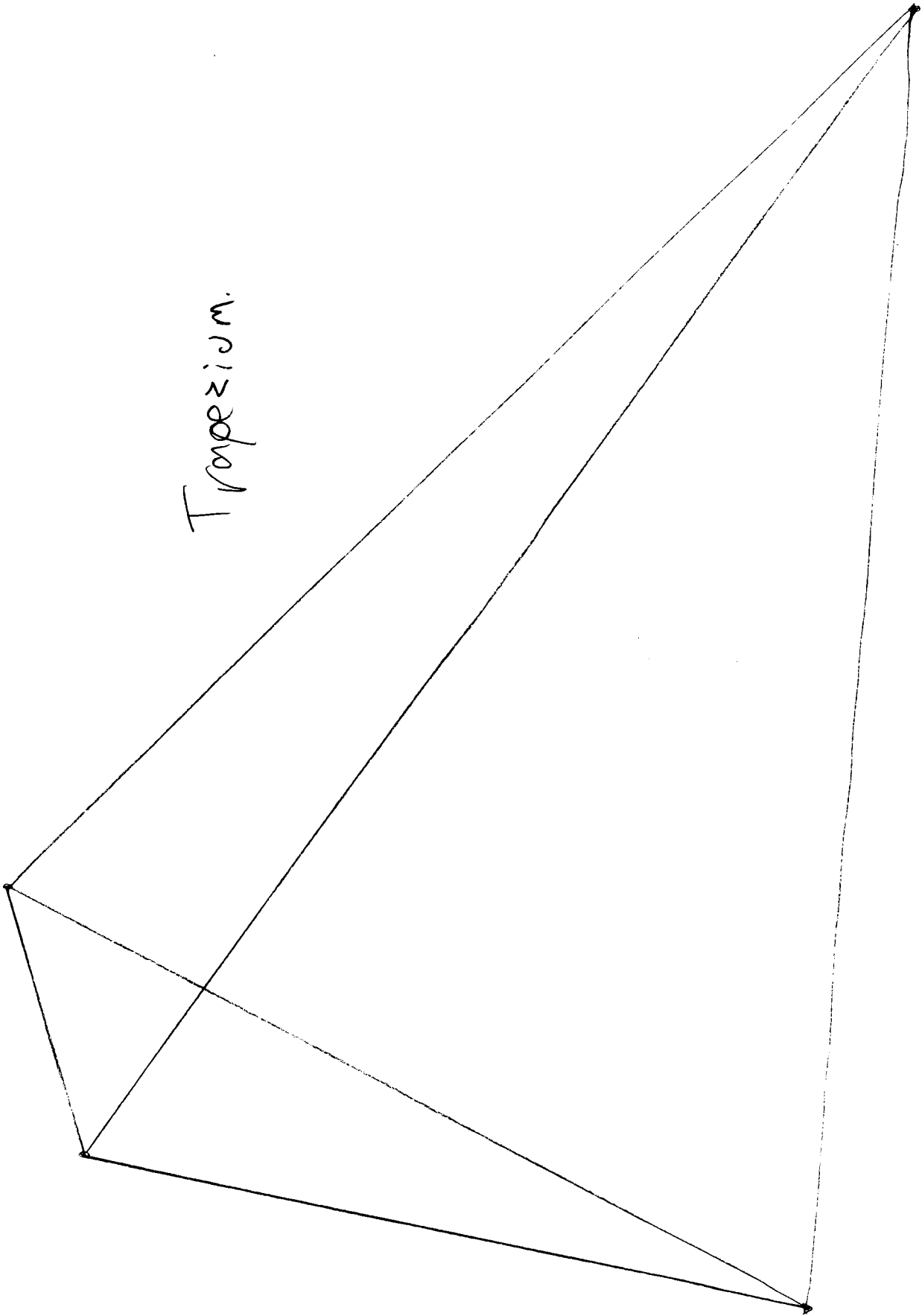
They need  
to cross  
each other.



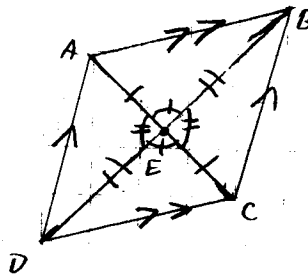
2



Trapezium.



Statements	Reasons
① E is the mid-point of $\overline{AC}$	① Given.
② E is the midpoint of $\overline{BD}$ .	② Given
③ $\angle AEB \cong \angle DEC$	③ Vertical angles
④ $\angle AED \cong \angle BEC$	④ Vertical angles
⑤ $\triangle DEC \cong \triangle BEA$	⑤ SAS
⑥ $\overline{AB} \parallel \overline{DC}$	



Alternate interior angles ~~proof~~ two lines to be parallel

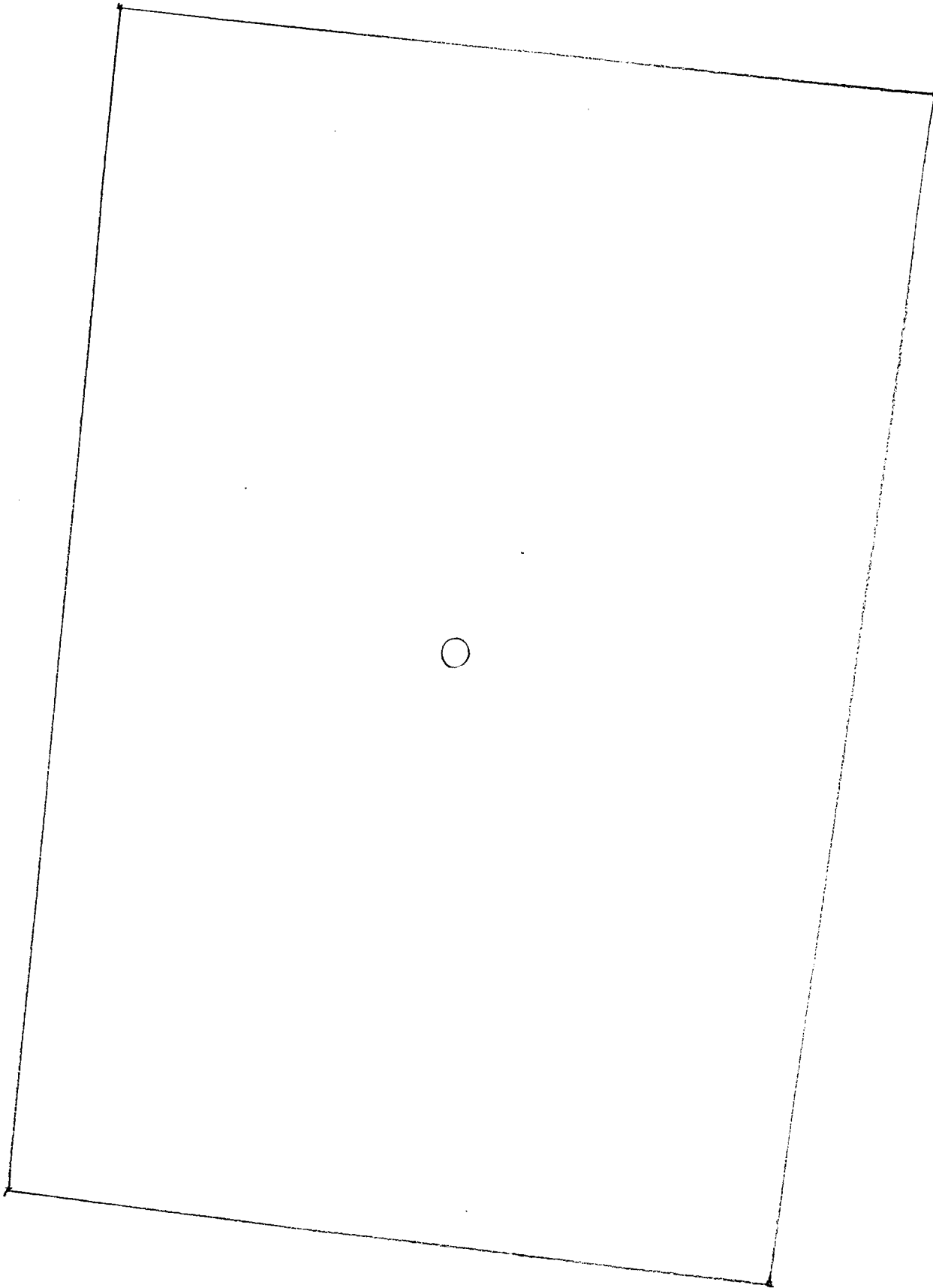


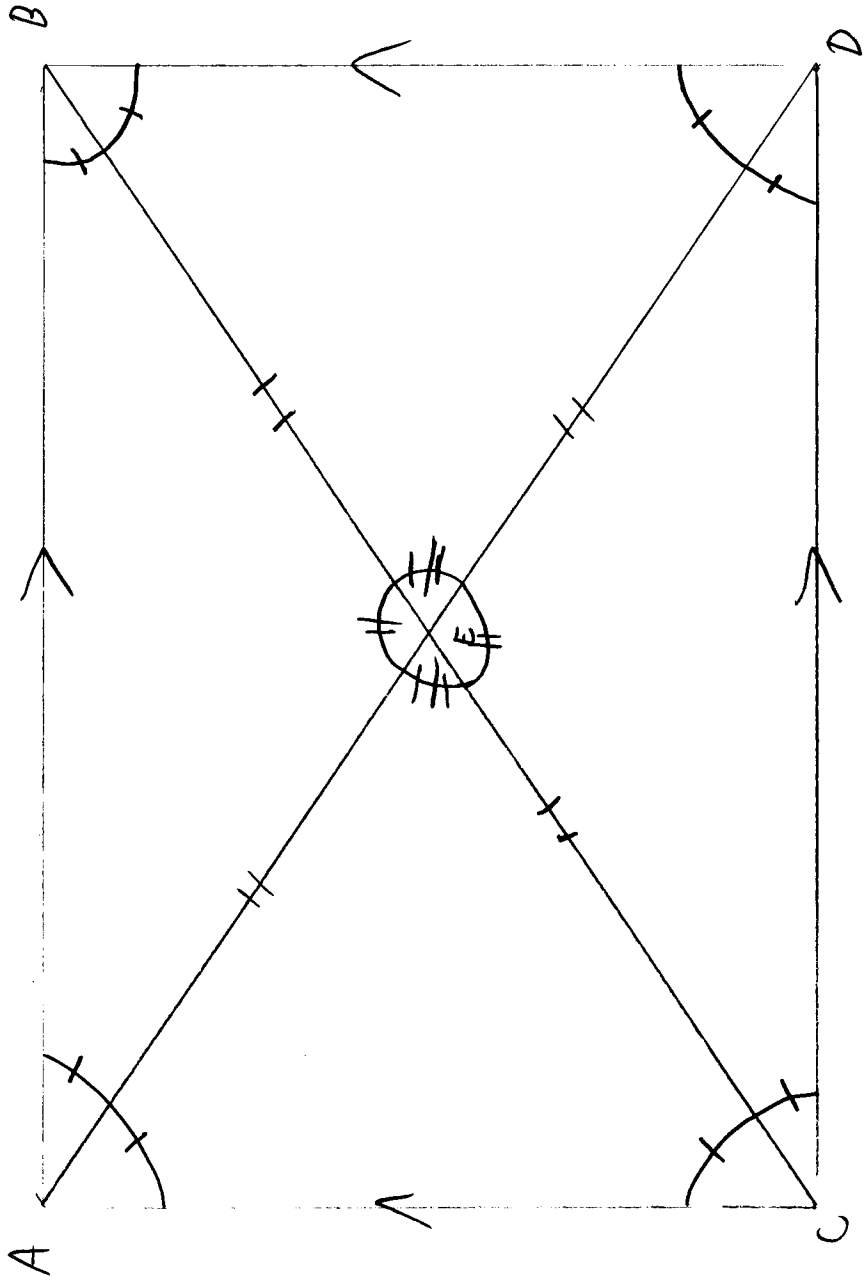
1. Use a compass to draw several circles. Each circle must have the same radius and the center of any new circle drawn must be on the circumference of an already existing circle. See what design you can create.

Statements	Reasons.
① $\overline{AD} \cong \overline{BC}$	① Given.
②	

2. Using the circles you've drawn construct an equilateral triangle (note: you may need to add more circles).

**Criteria:** *The circles need to be carefully constructed so that the radius does not change, even a little bit. Keep your pencil sharp, and make sure the intersections are precise. And the straight lines must be constructed with a straightedge! Keep practicing!*





- 
- How many shapes do we need to do?
  - How can we explain the diagonals on a trapezoid?
  - Do we have a lot of information or little?

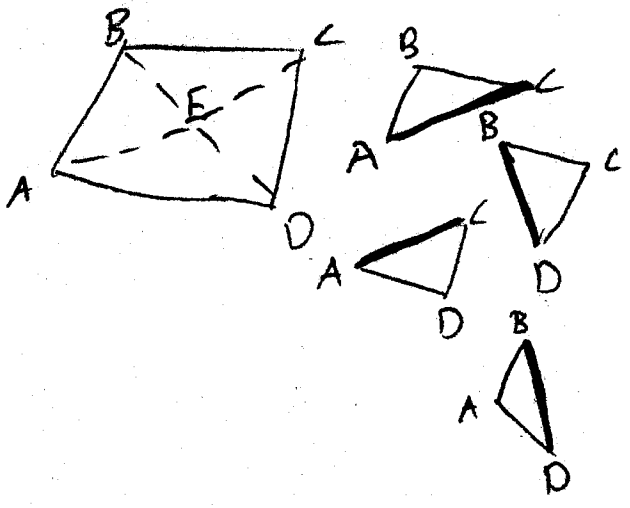
I think I did well when I was drawing the diagonals of each polygon. And finding the position of them.

I think I can improve by taking more notes and ideas so that I don't lose track of what I've done.

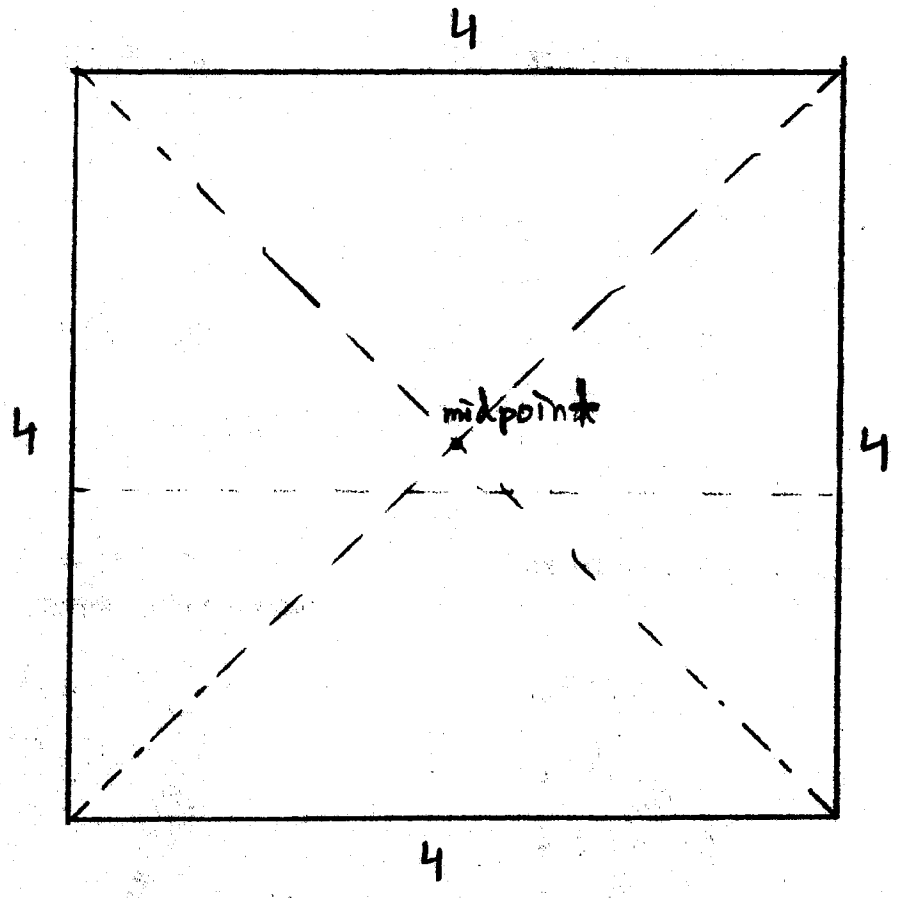
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All sticks have 9 holes;  $2(9^2)$  possibilities

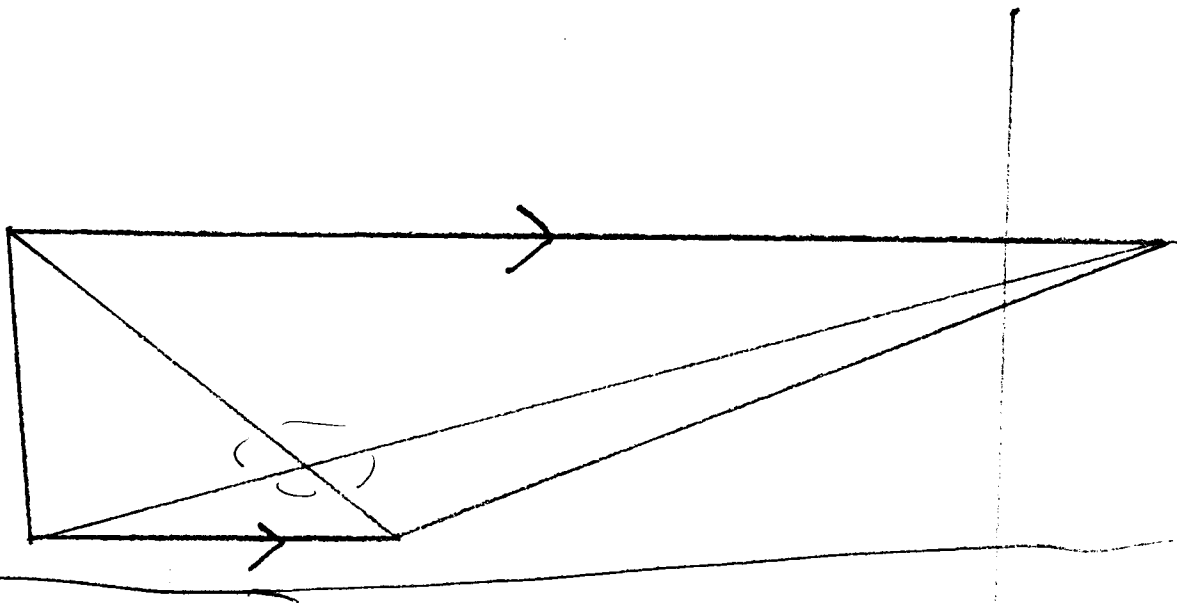
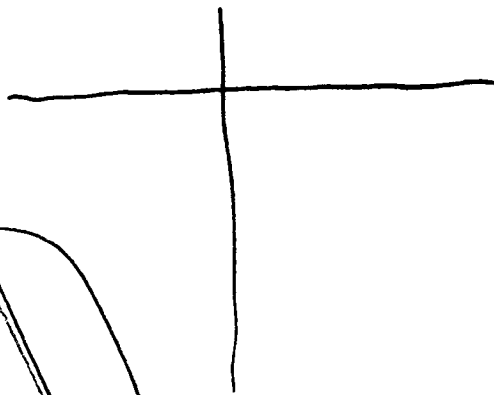
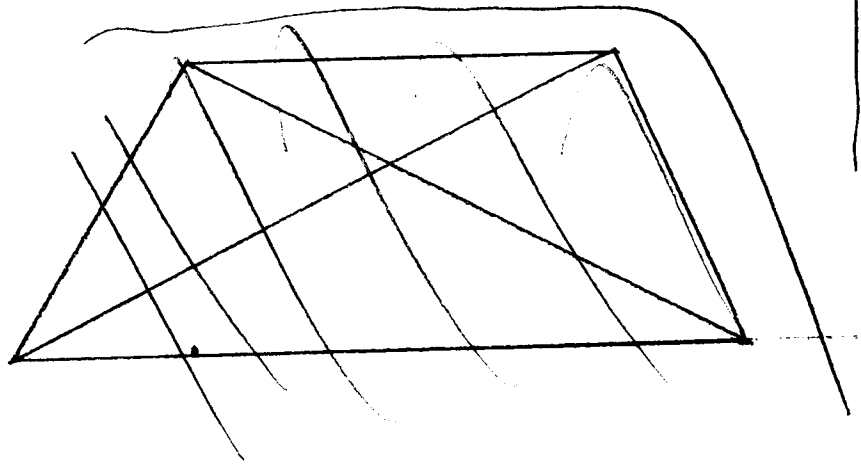
$$\frac{2(81)}{162}$$



Blk 1 3/3/09

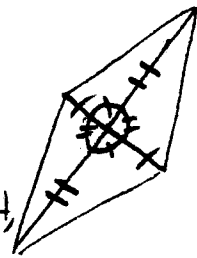






• diagonals bisect

• If a seg. is divided where the two new seg. are congruent, then the segment is bisected



• diagonals not perpendicular

• if supplementary angles are marked as 2 diff. lengths, then they are not perpendicular

If the diagonals bisect each other.

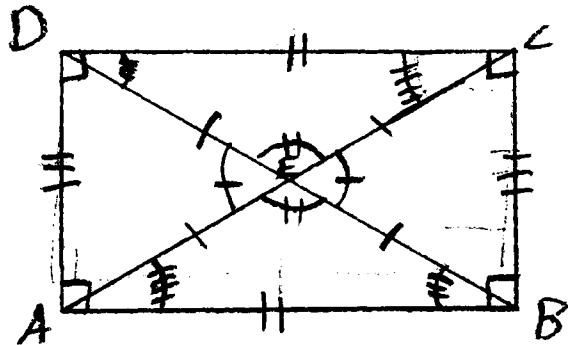
~~and the diagonals are not perpendicular~~

and the diagonals have same lengths

then the quadrilateral is a rectangle.

Rectangle: A parallelogram in which all angles are equal to  $90^\circ$ .

- |   |   |
|---|---|
| <ul style="list-style-type: none"><li>• <math>\triangle ABE \cong \triangle CED</math></li><li>• <math>\overline{CD} \cong \overline{AB}</math></li></ul> | <ul style="list-style-type: none"><li>• SAS</li><li>• CPCTC</li></ul> |
|---|---|



How do you solve for a trapezoid only with the diagonals?

I think I did well in drawing the shapes. But I think I can improve on writing down my thoughts.

### Kite



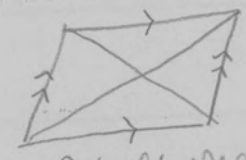
Sh  
lo

• only one stick can be in the center

• two lines always perpendicular

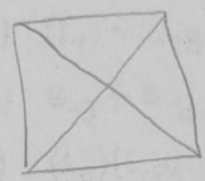
lo  
lo

### parallelogram



• square, rect  
• long stick short

### Square

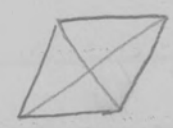


lo  
lo

• fastened middle of each line

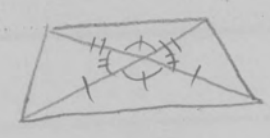
• same amount of holes on each side of line  
• lines perpendicular

### Rhombus



• short long - has to be perpendicular  
• long long -

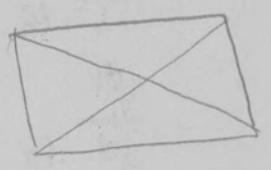
### trapezoid



• can't use center

~~• long short~~  
• long long  
• angle doesn't matter

### Rectangle



• fastened middle  
• doesn't have to be perpendicular

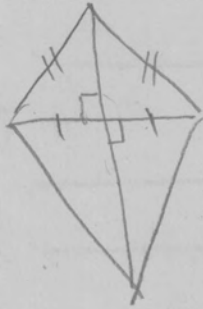


### Trapezium

• any two sticks in any hole

⊗ All - can't use top or bottom hole because that forms a triangle

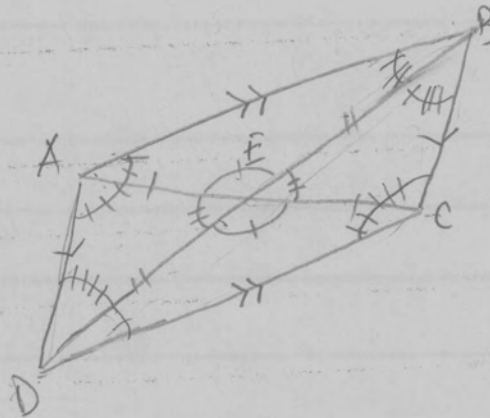
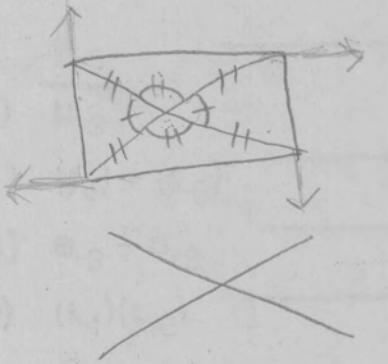
Kite



Non Iso Trap

- fastened at the same number hole
- can't be fastened in center

rectangle



Proof Parallelogram

Statement

Reason

①  $\triangle CED \cong \triangle AEB$

① SAS

②  $\triangle BEC \cong \triangle AED$

② SAS

③  $\angle BDC \cong \angle ABD$

③ CPCTC

⑤  $\overline{AB} \parallel \overline{DC}$

⑤ alternate interior angles

⑥  $\overline{AD} \parallel \overline{BC}$

⑥ alternate interior

④  $\angle BCA \cong \angle CAD$

④ CPCTC

---

How can we prove the rectangle's corners are  $90^\circ$  angles?

I think I did well in organizing my thoughts because each shape has its own section with observations. I think I can improve by using lines to separate the work so that two shapes' observations won't look like one. Write more notes.

---

trapezoid, kite, trapezium, rhombus, square, rectangle, parallelogram

1 long & 1 short

(or parallelogram)

center point on both can create a rhombus see a

center point on one can create a Kite see b

2 long

center point on both

square

c

rectangle

d

parallelogram

e

rhombus

f

center point on one

kite

g

center point on none, but same distance

trapezoids

h

**Rhombus**

center points on both sticks, any combination of sticks

**Kite**

center point on one stick, any combination of sticks

**Square**

center points on both sticks, both long sticks,  $90^\circ$  angles

**Parallelogram**

center points on both sticks, any combination of sticks

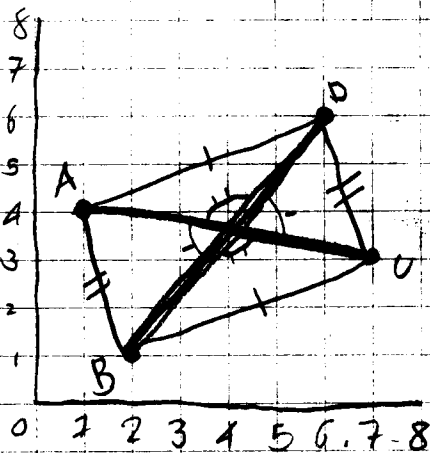
**Rectangle**

center points on both sticks, both long sticks

Trapezoid

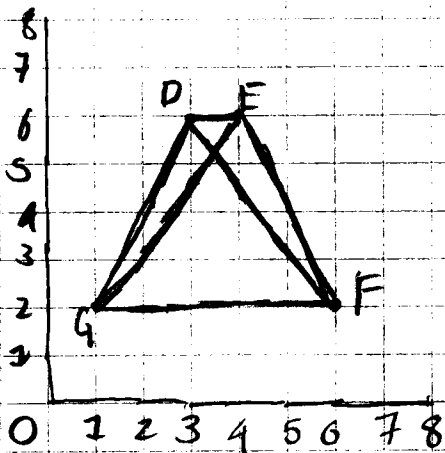
both points equidistant to endpoints, both long sticks





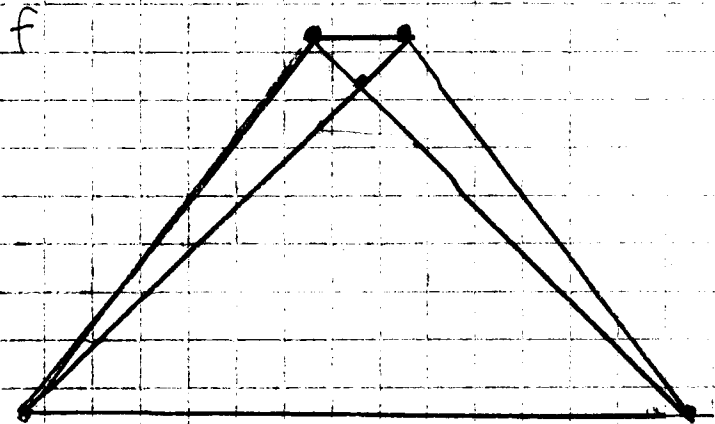
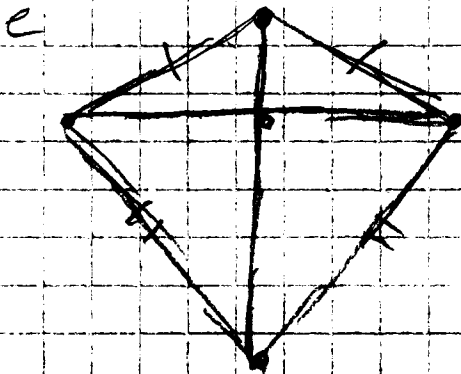
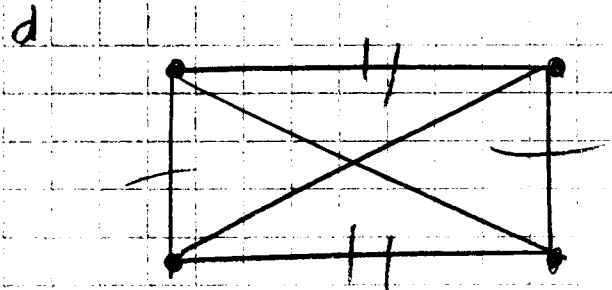
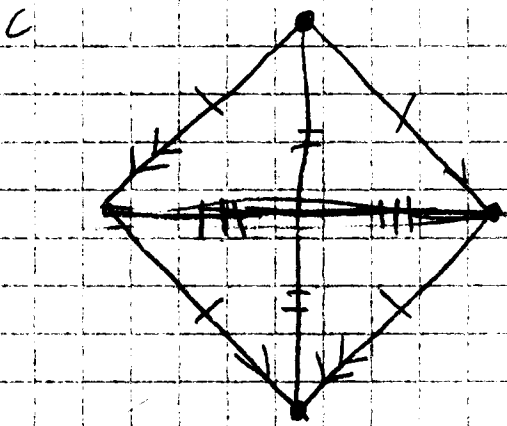
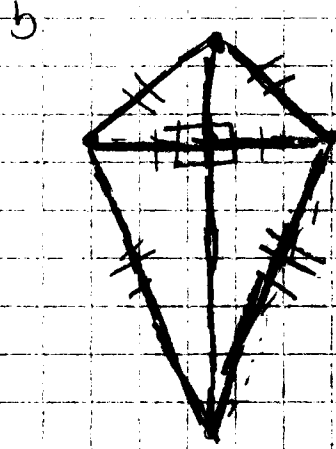
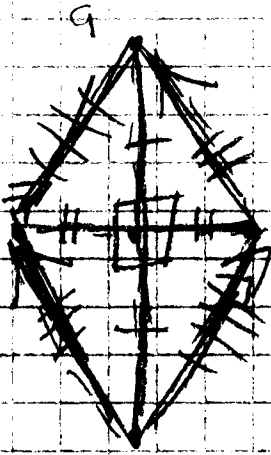
$$\begin{array}{l}
 A \left\{ \begin{array}{l} 1 \\ 4 \end{array} \right\} \\
 B \left\{ \begin{array}{l} 2 \\ 1 \end{array} \right\} \\
 C \left\{ \begin{array}{l} 7 \\ 3 \end{array} \right\} \\
 D \left\{ \begin{array}{l} 6 \\ 6 \end{array} \right\}
 \end{array}
 \quad
 \begin{array}{l}
 \frac{3-1}{7-2} = \frac{2}{5} \\
 \frac{6-4}{6-1} = \frac{2}{5} \\
 \frac{4-1}{1-2} = \frac{3}{-1} = -3 \\
 \frac{6-3}{6-7} = \frac{3}{-1} = -3
 \end{array}$$

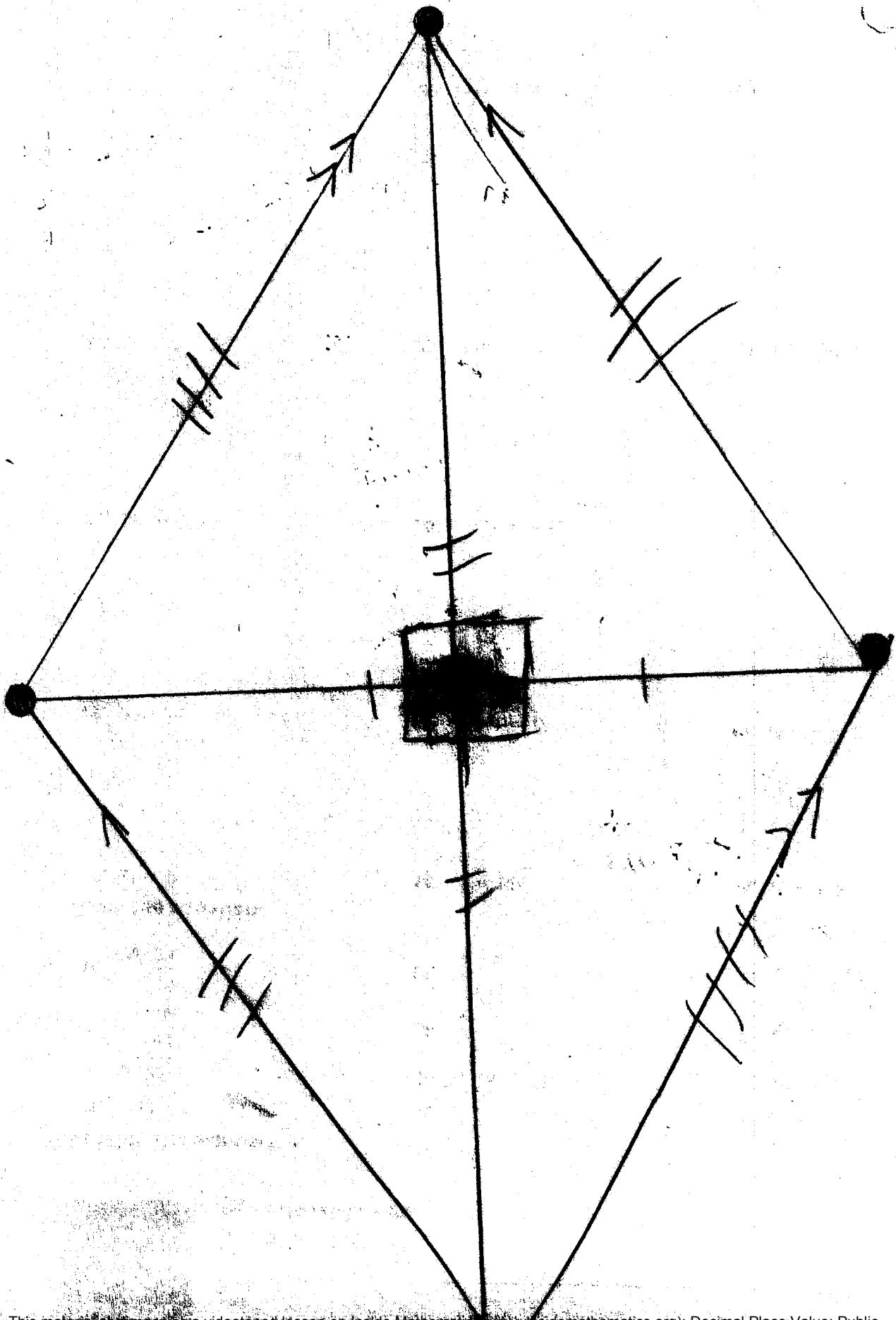
Statements	Reasons
$m$ for BC is $\frac{2}{5}$	slope formula and points
$m$ for AD is $\frac{2}{5}$	slope formula and points
$AD \parallel BC$	slopes are =
$m$ for AB is -3	slope formula and points
$m$ for CD is -3	slope formula and points
$AB \parallel CD$	slopes are =
$\square ABCD$ is a parallelogram	def. of parallelogram

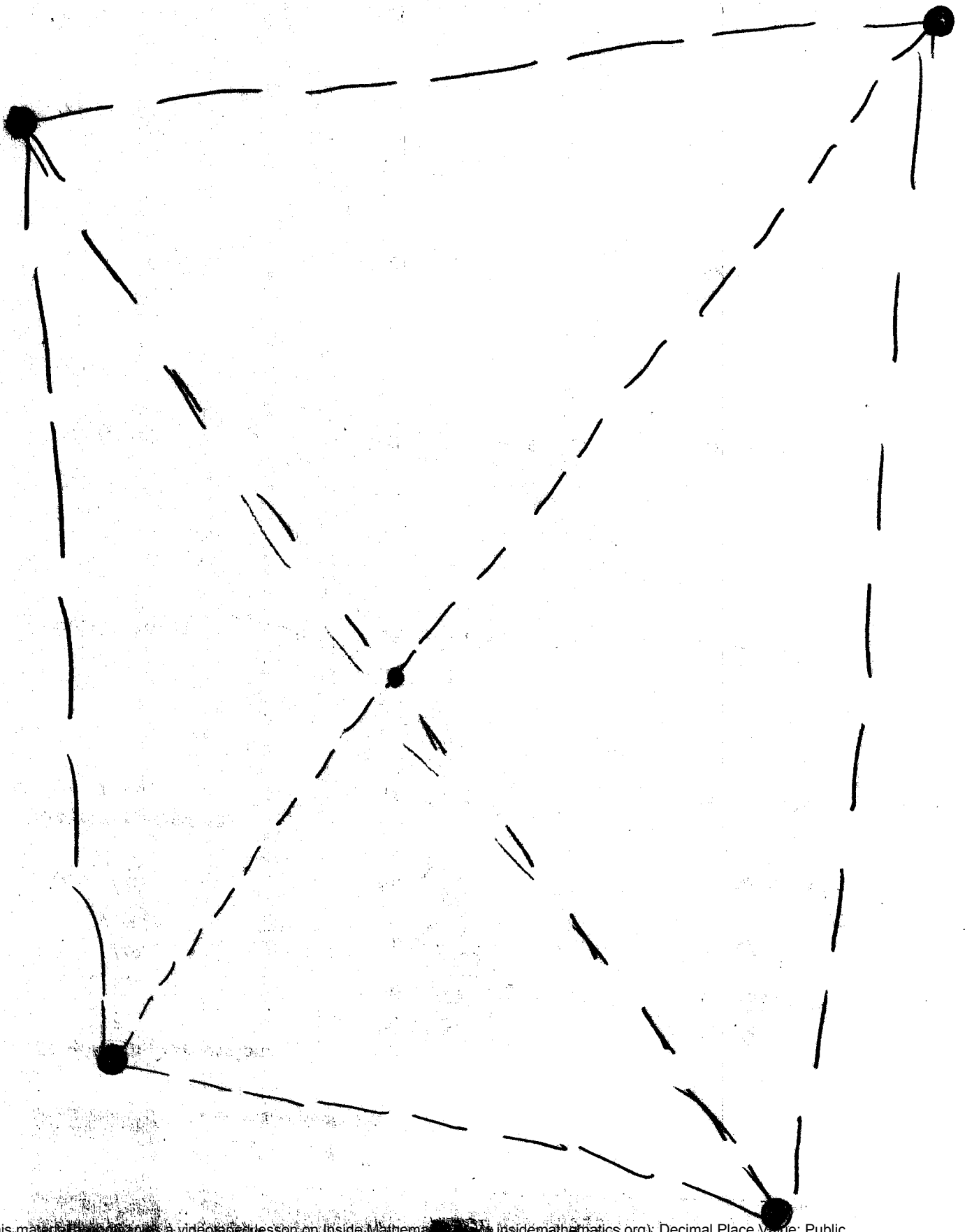


$$\begin{array}{l}
 D \left\{ \begin{array}{l} 3 \\ 6 \end{array} \right\} \\
 E \left\{ \begin{array}{l} 4 \\ 6 \end{array} \right\} \\
 F \left\{ \begin{array}{l} 6 \\ 2 \end{array} \right\} \\
 G \left\{ \begin{array}{l} 1 \\ 2 \end{array} \right\}
 \end{array}
 \quad
 \begin{array}{l}
 \frac{6-6}{4-3} = \frac{0}{1} = 0 \\
 \frac{2-2}{6-1} = \frac{0}{5} = 0
 \end{array}$$

Statements	Reasons
$m$ for ED is 0	slope formula and points
$m$ for FG is 0	slope formula and points
$ED \parallel FG$	slopes are =
$\square DEFG$ is a trap.	def. of trap.







Bl. 1 3-3-09

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Which sticks have the most shapes that can be made?

Why doesn't the kite make, not make custom orders?

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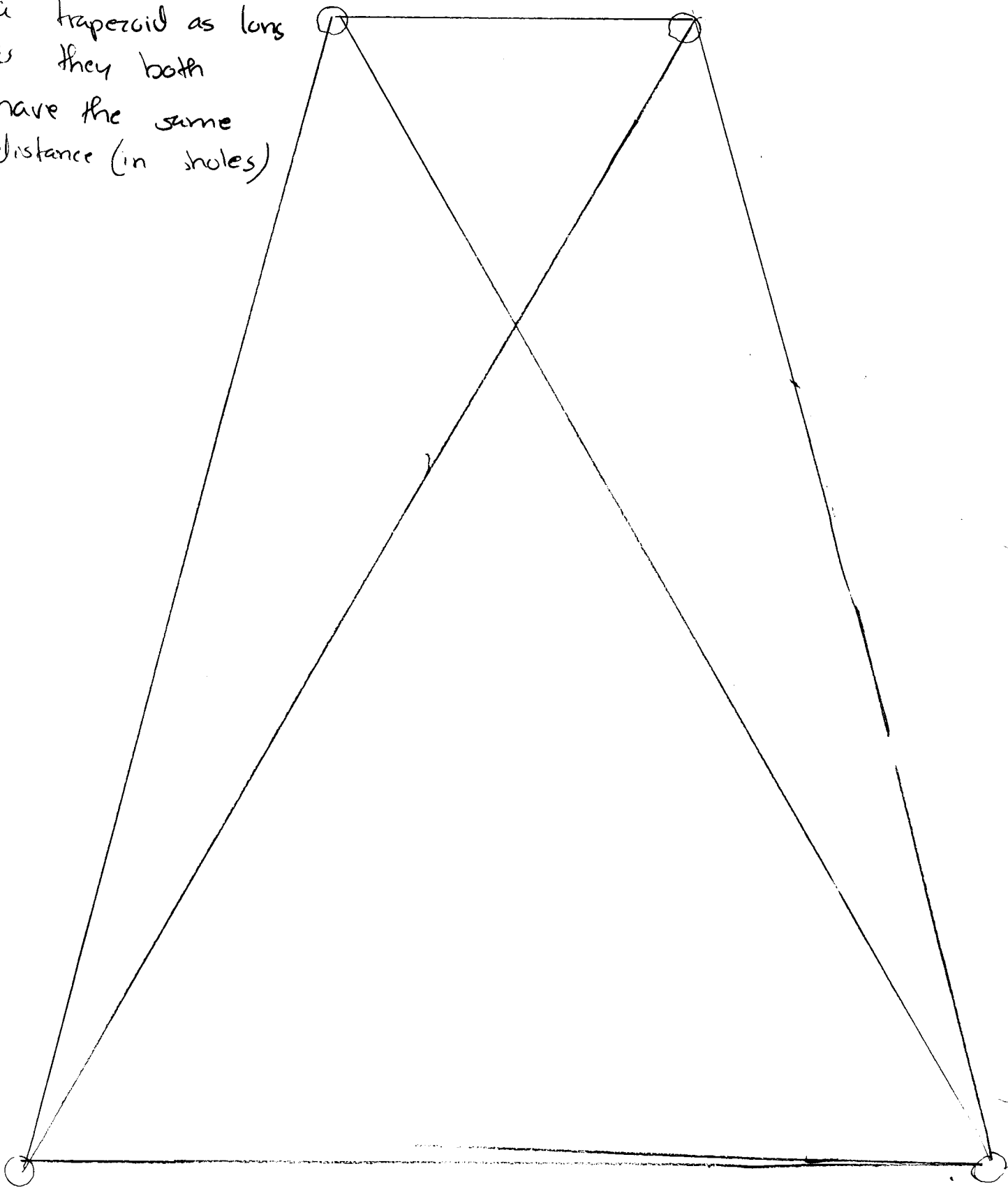
What I think I did well:  
getting information on the paper about the shapes  
we made.

What I think I could improve next time:  
being specific & clear in my data.

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# 1. Trapezoid (?)

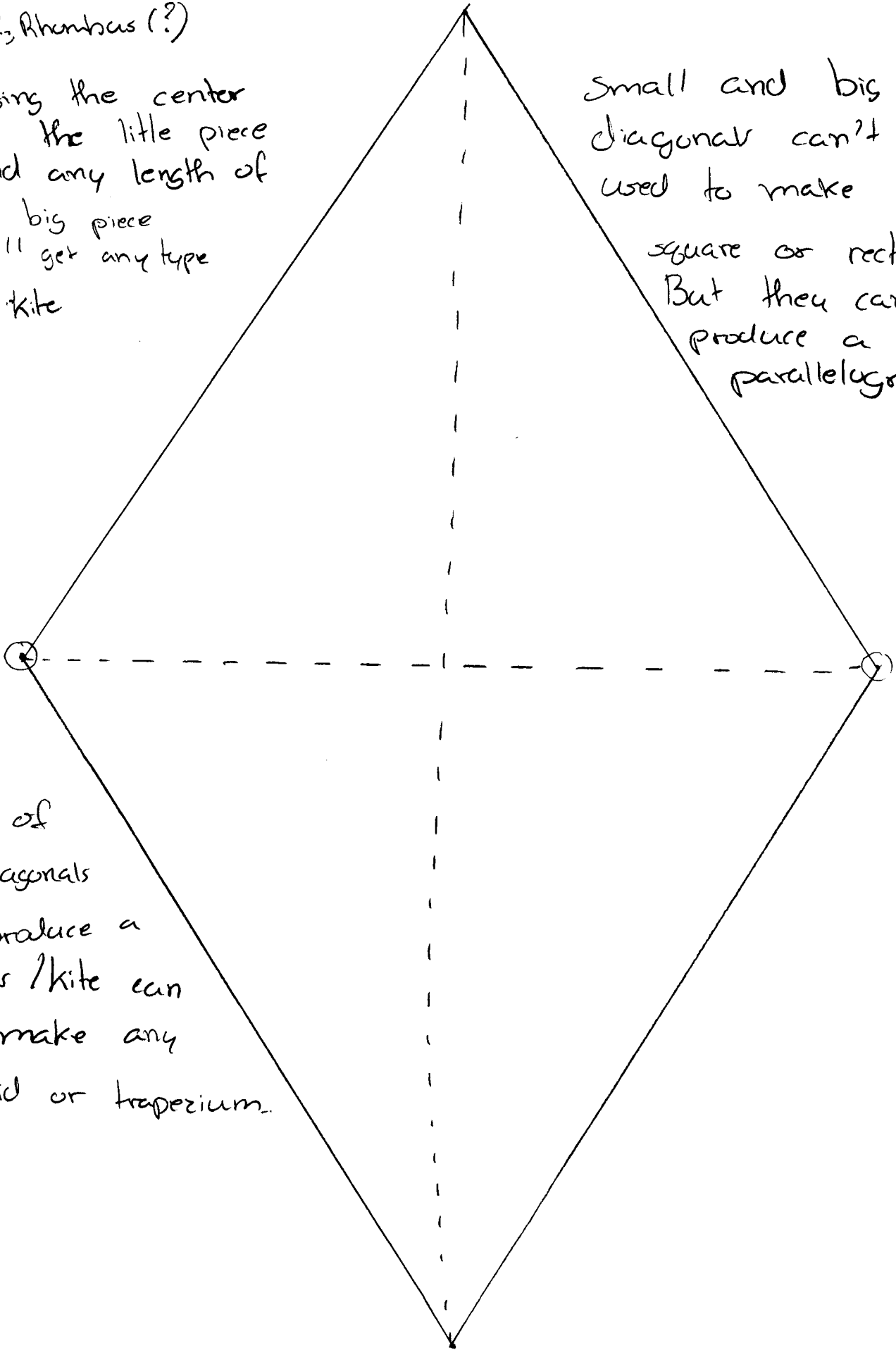
Using the two big pieces,  
you can make  
a trapezoid as long  
as they both  
have the same  
distance (in holes)



2, Rhombus (?)

using the center  
of the little piece  
and any length of  
the big piece  
you'll get any type  
of kite

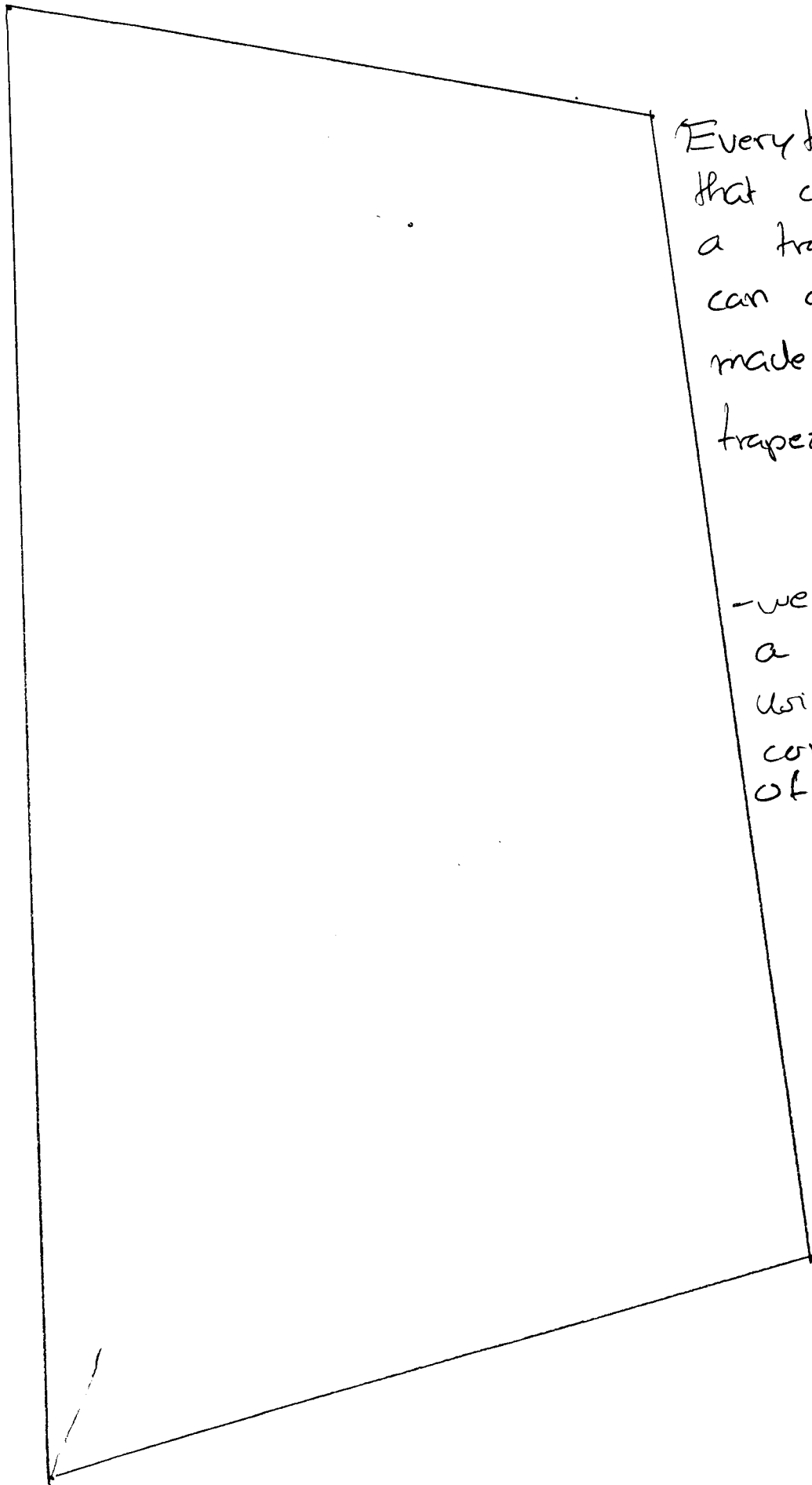
Small and big  
diagonal can't be  
used to make a  
square or rectangle.  
But they can  
produce a  
parallelogram.



Any of  
the diagonals  
that produce a  
rhombus / kite can  
also make any  
trapezoid or trapezium.



### 3. Trapezium



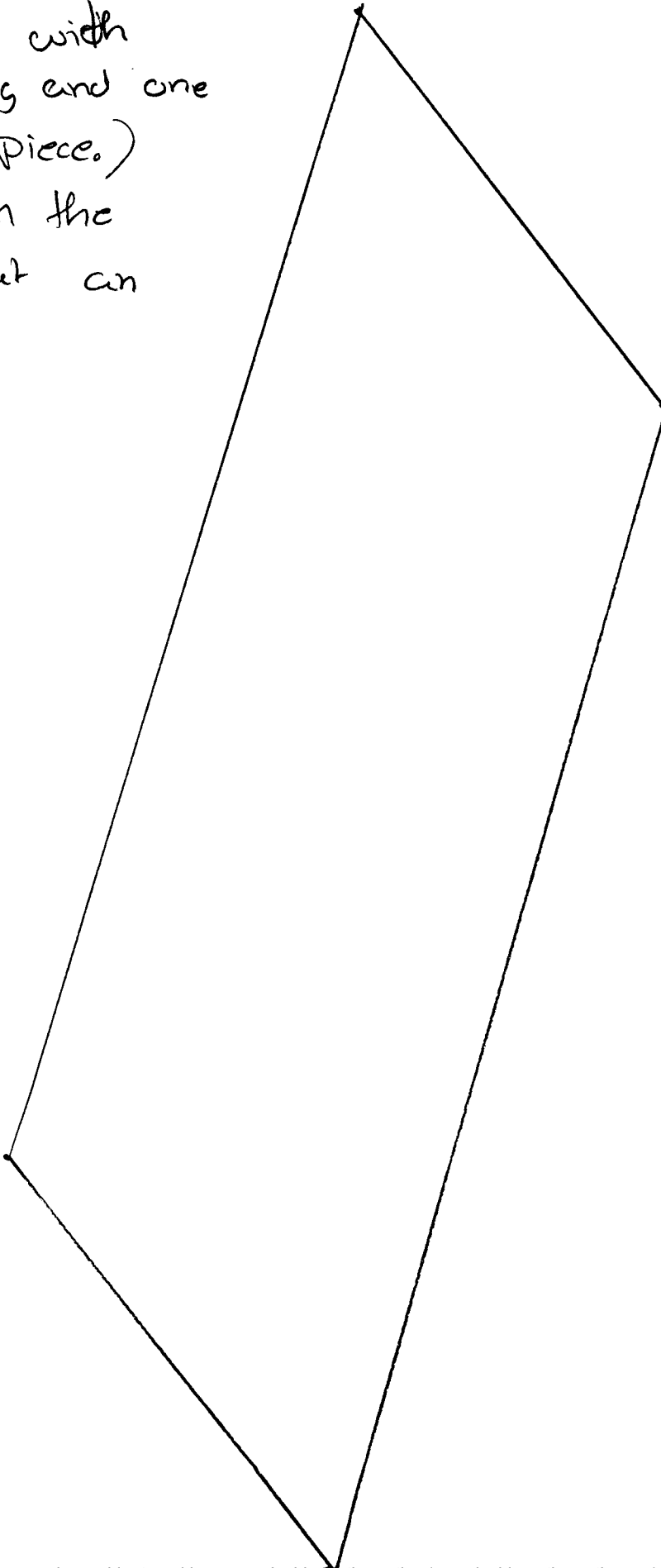
Everything that can make a trapezoid can also be made into a trapezium.

-we can produce a trapezium using any combination of diagonals.

#### 4. Parallelogram

(Made with  
one big and one  
small piece.)

Both in the  
center at an  
angle



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I wonder if we can produce  
any other quadrilaterals using all  
three of the pieces other than a  
trapezoid

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I think that we did good as a group because when ever we found out about something that was new we shared it with the group and wrote it down.

I think I can improve by thinking more about the work geometrically over too much tinkering.

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